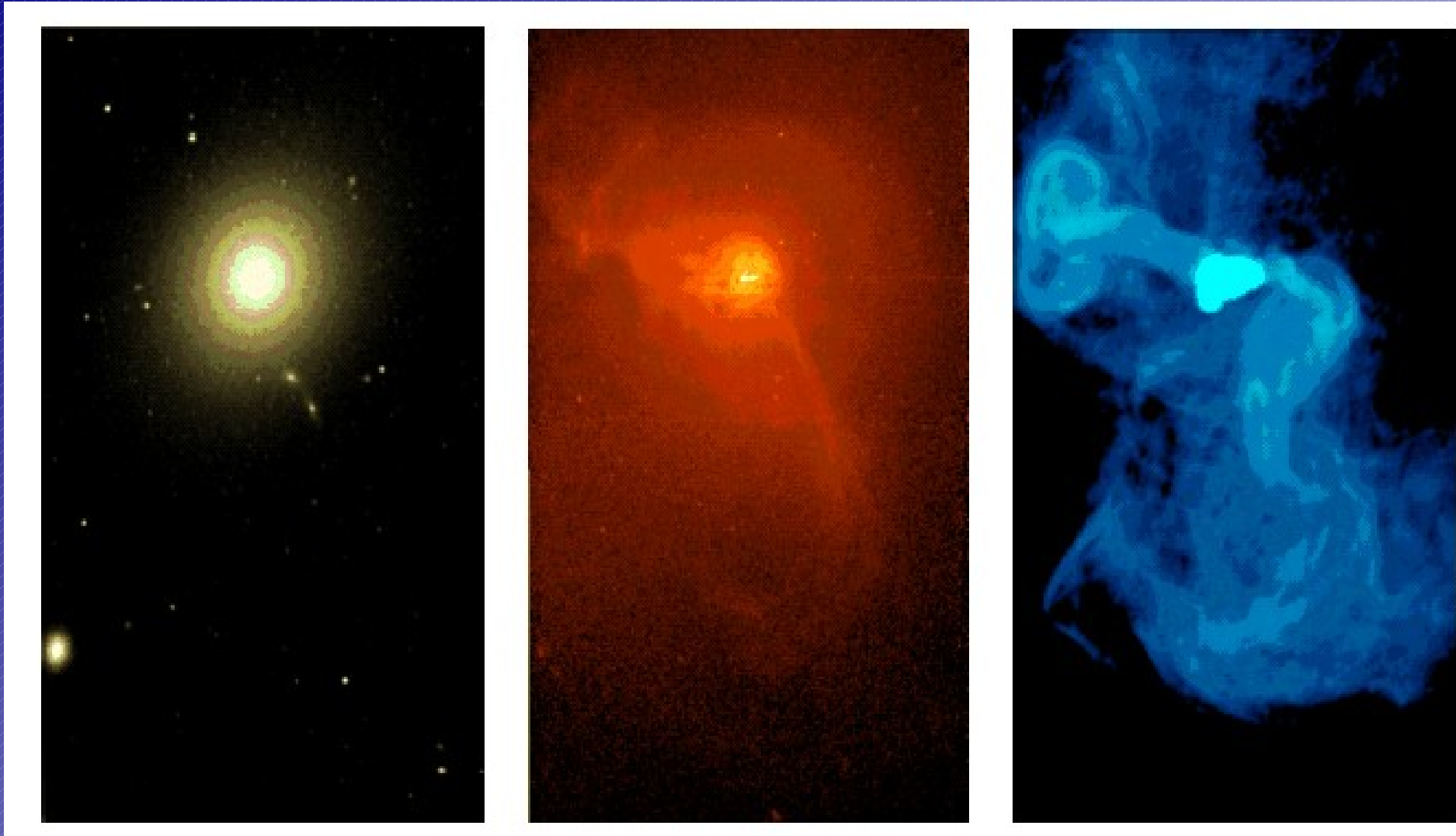


# Ellipticals cont.

- Modern view
  - Ellipticals can be complex systems
    - X-ray gas and dust lanes
    - Some have young stars
      - Often in a dynamically distinct disk
    - Some ellipticals have significant rotation
    - Formation is a more complex process, merger of two spirals? Hierarchical accretion of smaller ellipticals? Both?



M87 in the optical X-ray and radio and at the same scale.

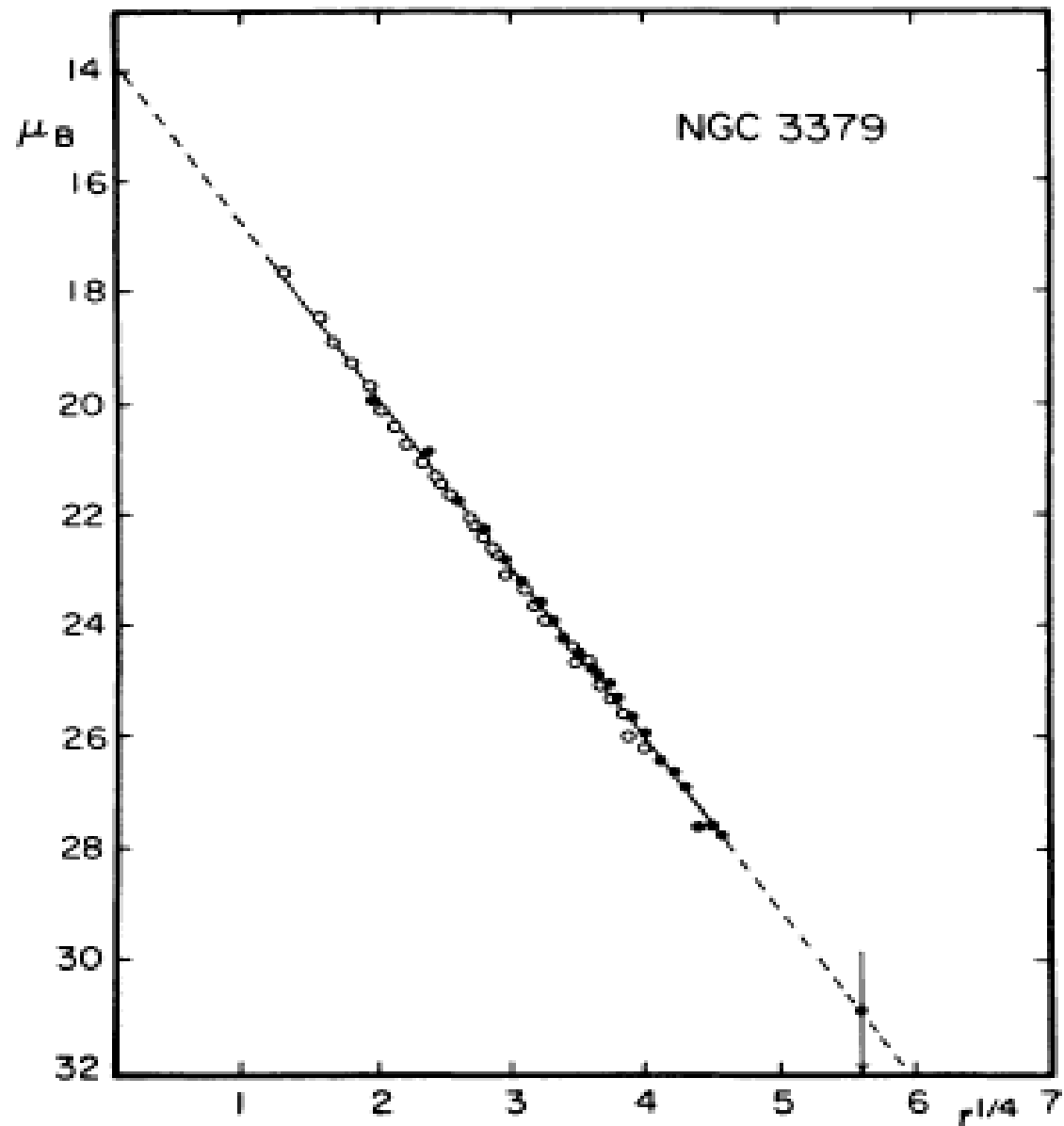
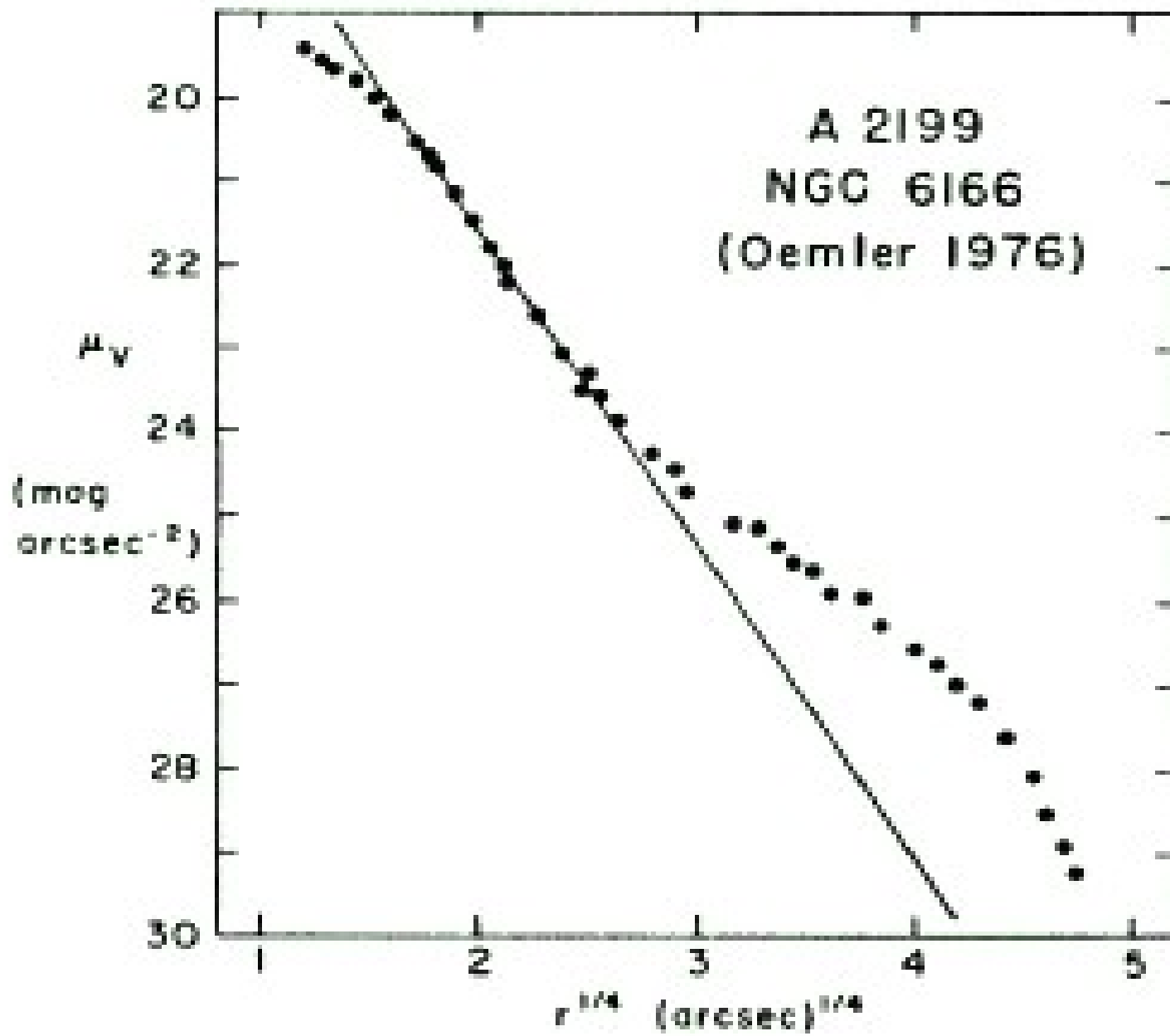


FIG. 2.—Mean E-W luminosity profile of NGC 3379 derived from McDonald photoelectric data. ●, Pe 4 data with 90 cm reflector; ○, Pe 1 data (M + P) with 2 m reflector. Note close agreement with  $r^{1/4}$  law.





So an observer looking along the z axis would see an E0 (round) galaxy, when viewed at an angle you would see an elliptical shape with apparent axis ratio  $q = b/a$ . Looking at the tangent point to the elliptical surface (T) the coordinates of this point are

$$\tan i = \frac{dx}{dz} = -\left(\frac{z}{x}\right)\left(\frac{A^2}{B^2}\right)$$

The elliptical image of this surface has a semi-major axis of  $a = mA$  and the semi-minor axis  $b$  is  $OR$  and this is also  $OQ \sin(i)$ . So from the equations above we can write

$$OQ = OP + PQ = z + (-x) \cot(i) = \frac{B^2 m^2}{z};$$

# Distribution of B/A

Looking from a random direction what fraction of galaxies do we see between  $i$  and  $i+\Delta i$ ? It's just  $\sin(i) \Delta i$   
So if all galaxies have an axial ratio of  $B/A$  then the fraction with apparent ratios between  $q$  and  $q + \Delta q$  is

$$f_{obl}(q) \Delta q = \frac{\sin(i) \Delta q}{dq/di} = \frac{q \Delta q}{\sqrt{1-(B/A)^2} \sqrt{q^2-(B/A)^2}}$$

For very flattened systems,  $B \ll A$  the distribution is almost uniform

# Distribution of B/A cont.

- The disks of spiral and S0 galaxies the apparent shapes with  $q \approx 0.2$  are found with equal probability.
  - So we conclude that in general their disks have  $B/A \leq 0.2$
  - We see very few spirals with  $q \leq 0.1$  which means that very few spirals have  $B/A \approx 0.1$
- No ellipticals flatter than E7 ( $q=0.3$ )
  - Dynamically unstable?



# Isophotal Shapes

- While elliptical galaxy isophotes are close to ellipses small deviations do occur
- We see
  - Twisting isophotes
  - Disky isophotes
  - Boxy isophotes

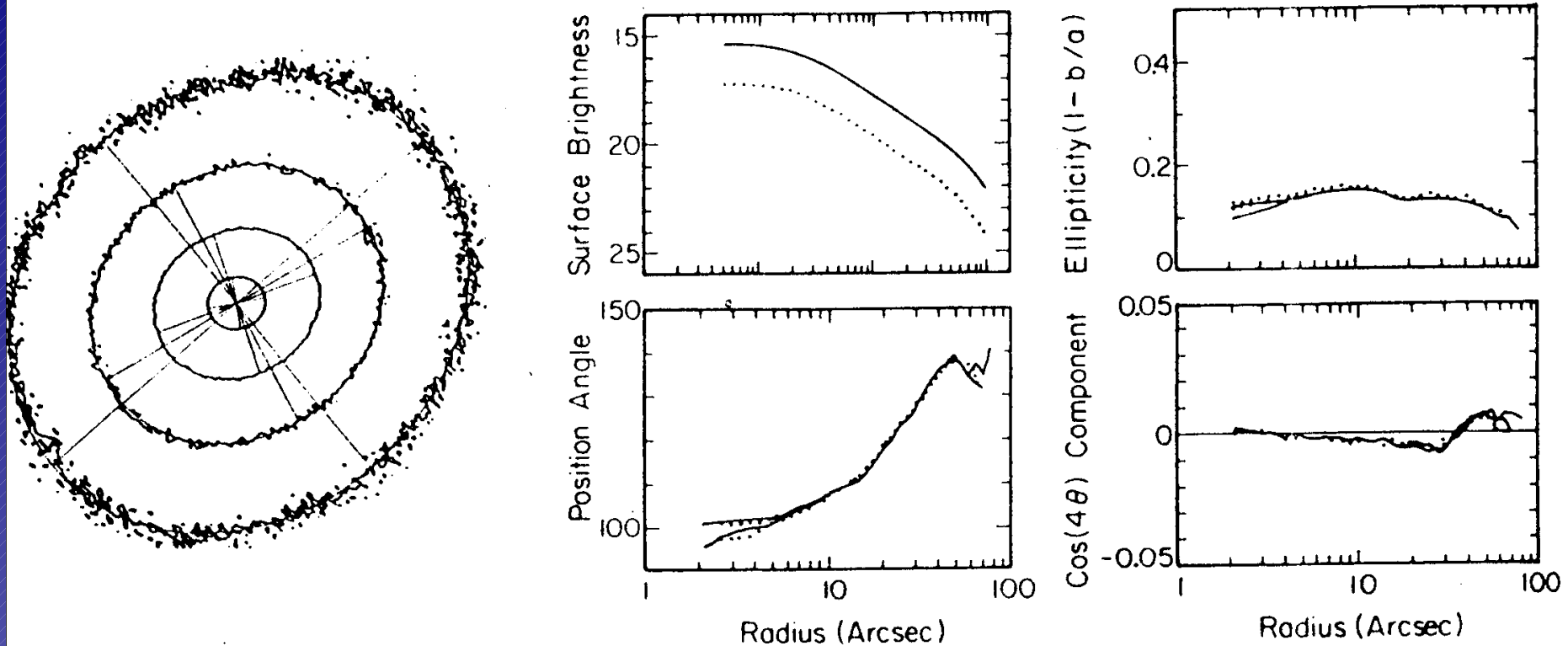
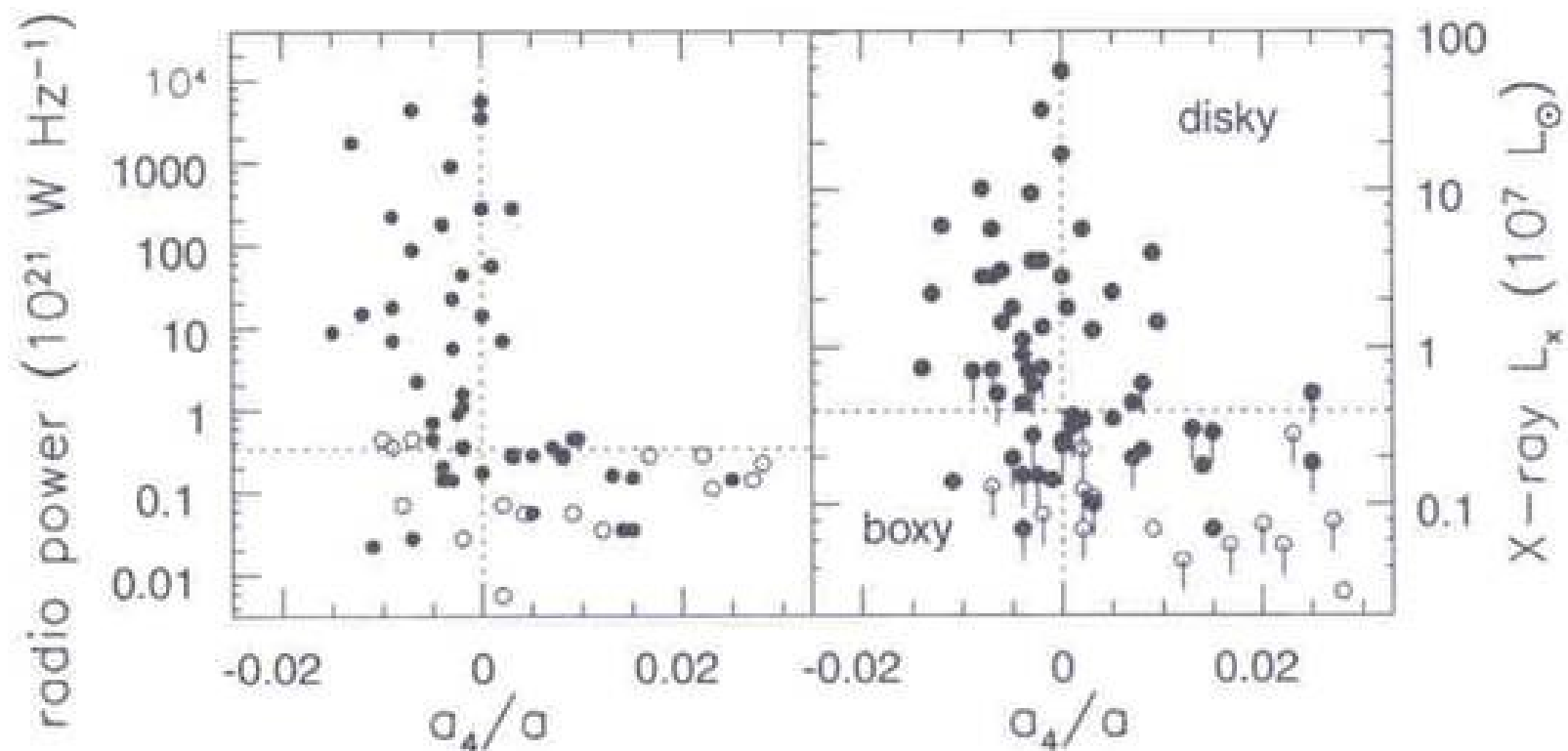


Figure 1: *Surface brightness distribution of the elliptical galaxy NGC 1549, taken from Jedrzejewski (1987). The left panel gives a contour map with the major and the minor axes overlaid. The four right hand panels give the surface brightness, the ellipticity  $\epsilon$ , the position angle  $PA$ , and the  $\cos 4\theta$  variation of the surface brightness along the best fitting elliptic isophote, all as a function of radius. The solid lines show the measurements in the R band, while the dotted lines refer to the B band.*



**Figure 6.11** Radio and X-ray power of elliptical galaxies. Boxy galaxies, with  $a_4 < 0$ , tend to be strong sources; diskly ellipticals, with  $a_4 > 0$ , are usually weak. Filled circles show bright objects, with  $M_B < -19.5$ ; open circles are dimmer galaxies. Points with downward-extending bars show upper limits on the X-ray emission; luminosities are calculated for  $H_0 = 75 \text{ km s}^{-1} \text{ Mpc}^{-1}$  – R. Bender.

# Shell Galaxies

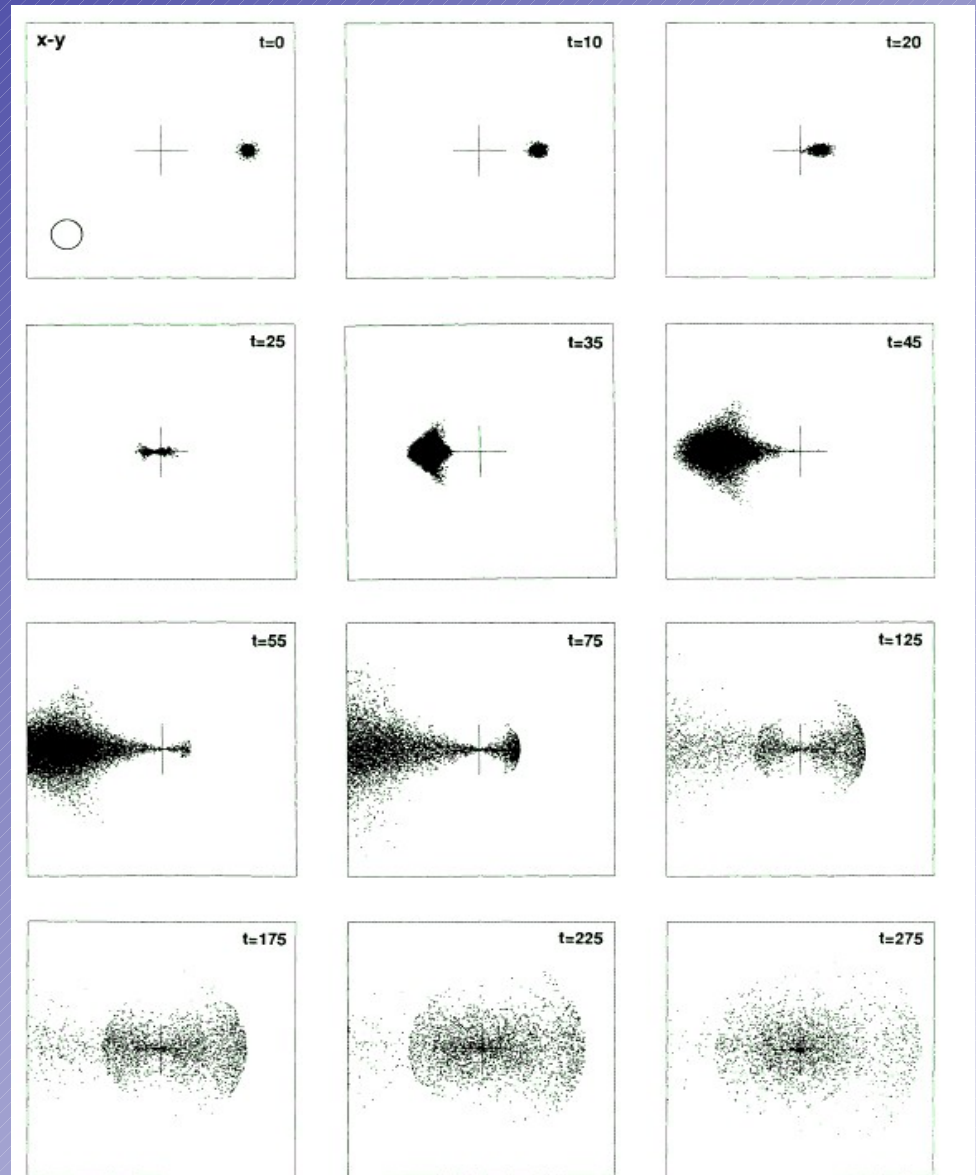
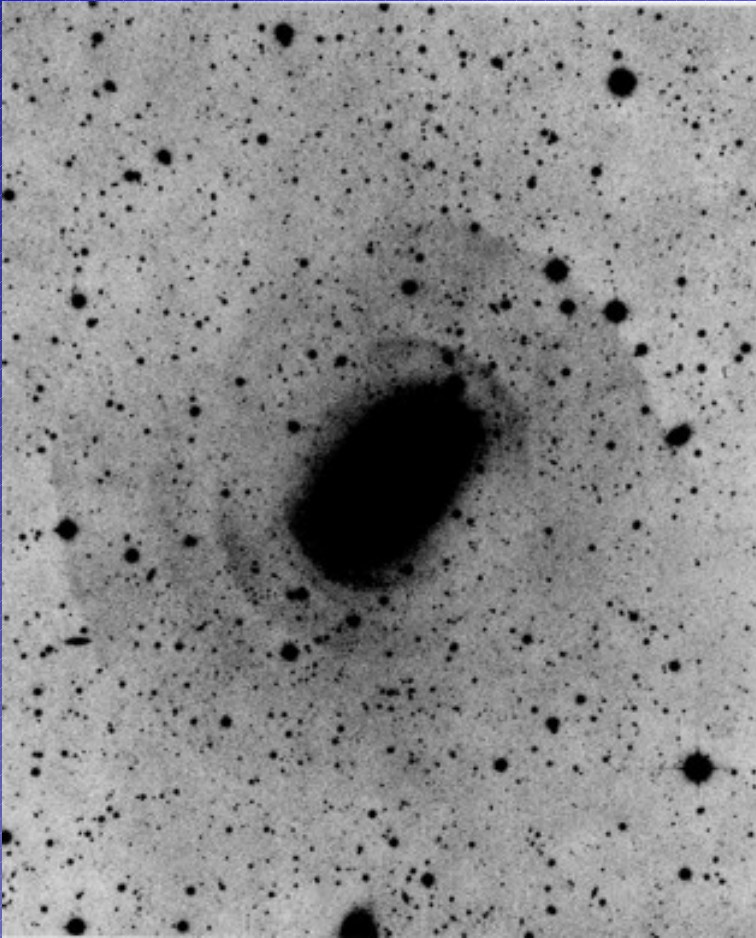


Figure 1. A radial encounter between a spherical Plummer primary and a spherical companion. The companion mass was 0.01 and its half-mass radius was 0.2 (both 1 for primary). The circle in the first frame indicates a spherical primary was used and the cross is at the center-of-mass.

- The rotational velocity for NGC 1399
  - $\Delta v \sim 100$  km/s
  - $\sigma_r$  is between 250 - 400 km/s
  - So  $V_{\max} / \sigma_r < 1$ 
    - Spirals have  $V_{\max} \approx 10\sigma_r$
  - So ellipticals are “slow” rotators

# Kinematics of Ellipticals

- $V_{\text{rot}}/\sigma$  correlates with luminosity
  - Lower luminosity ellipticals have higher  $V_{\text{rot}}/\sigma$  , rotationally supported
  - Higher luminosity ellipticals have lower  $V_{\text{rot}}/\sigma$  -- pressure supported
- $V_{\text{rot}}/\sigma$  correlates with boxy/diskiness
  - Disky ellipticals have higher  $V_{\text{rot}}/\sigma$  -- rotationally supported
  - Boxy ellipticals have lower  $V_{\text{rot}}/\sigma$  -- pressure supported

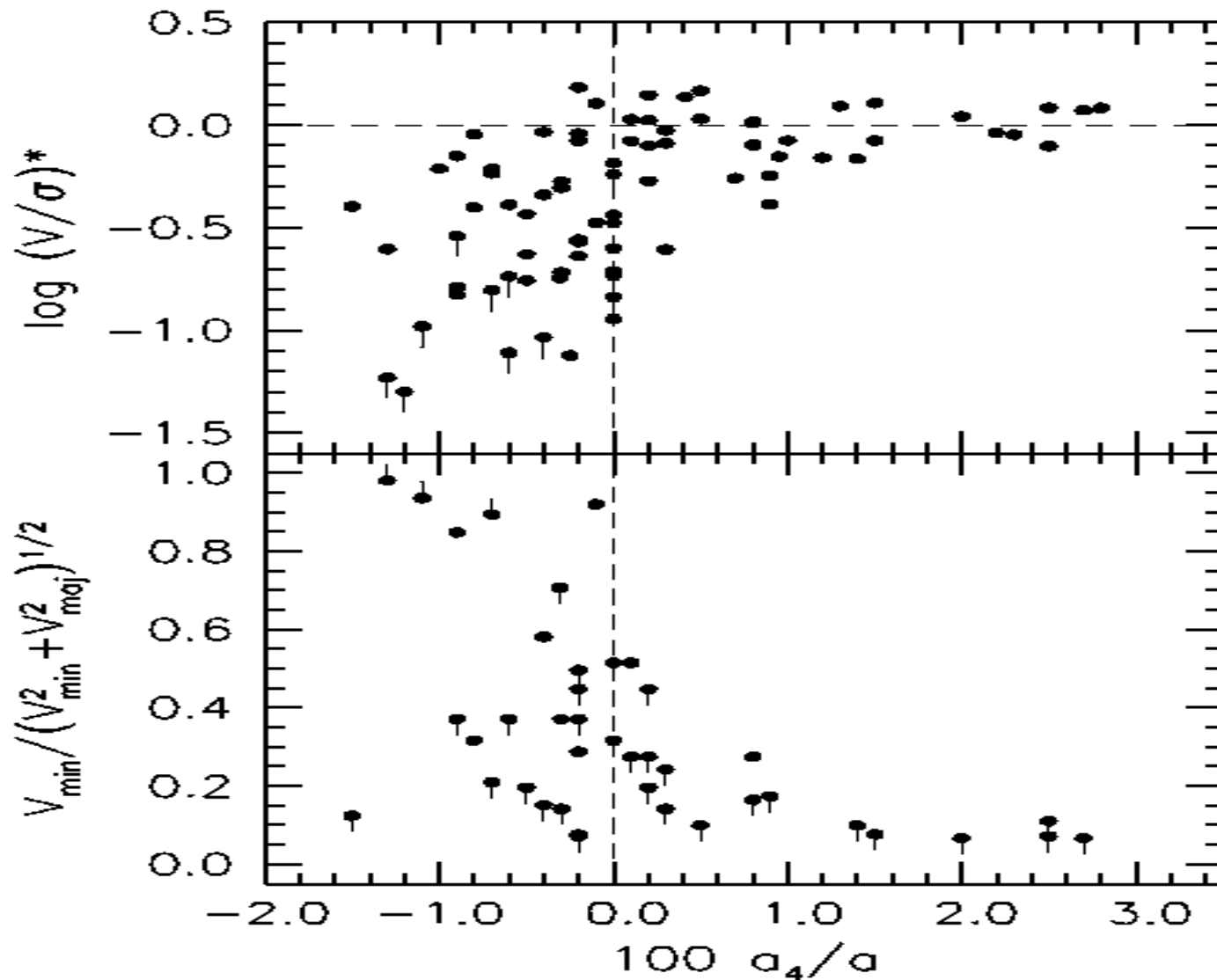


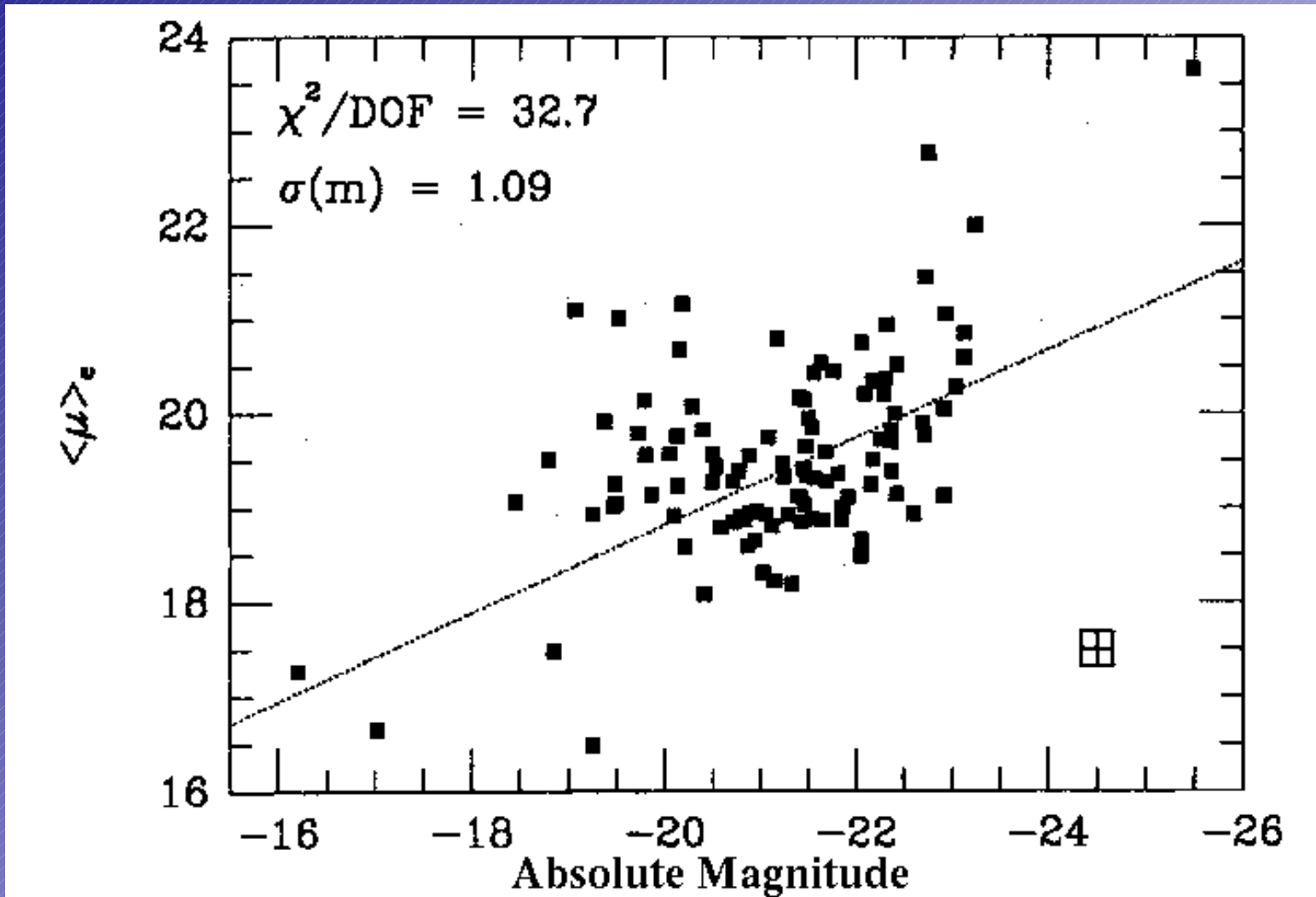
FIG. 2.—Correlations with isophote shape of parameters that are diagnostic of velocity anisotropy. Here  $100 a_4/a$  is the percent inward or outward perturbation of isophote radii along the major axis; negative values imply boxy isophotes; positive values imply disky isophotes. The upper panel shows the rotation parameter  $(V/\sigma)^*$  (from Bender 1988, with  $a_4/a$  values from B+89 and with  $(V/\sigma)^*$  values added from Davies *et al.* 1983). The lower panel shows maximum minor-axis rotation velocities normalized by total rotation velocity.

# Elliptical Isophotes

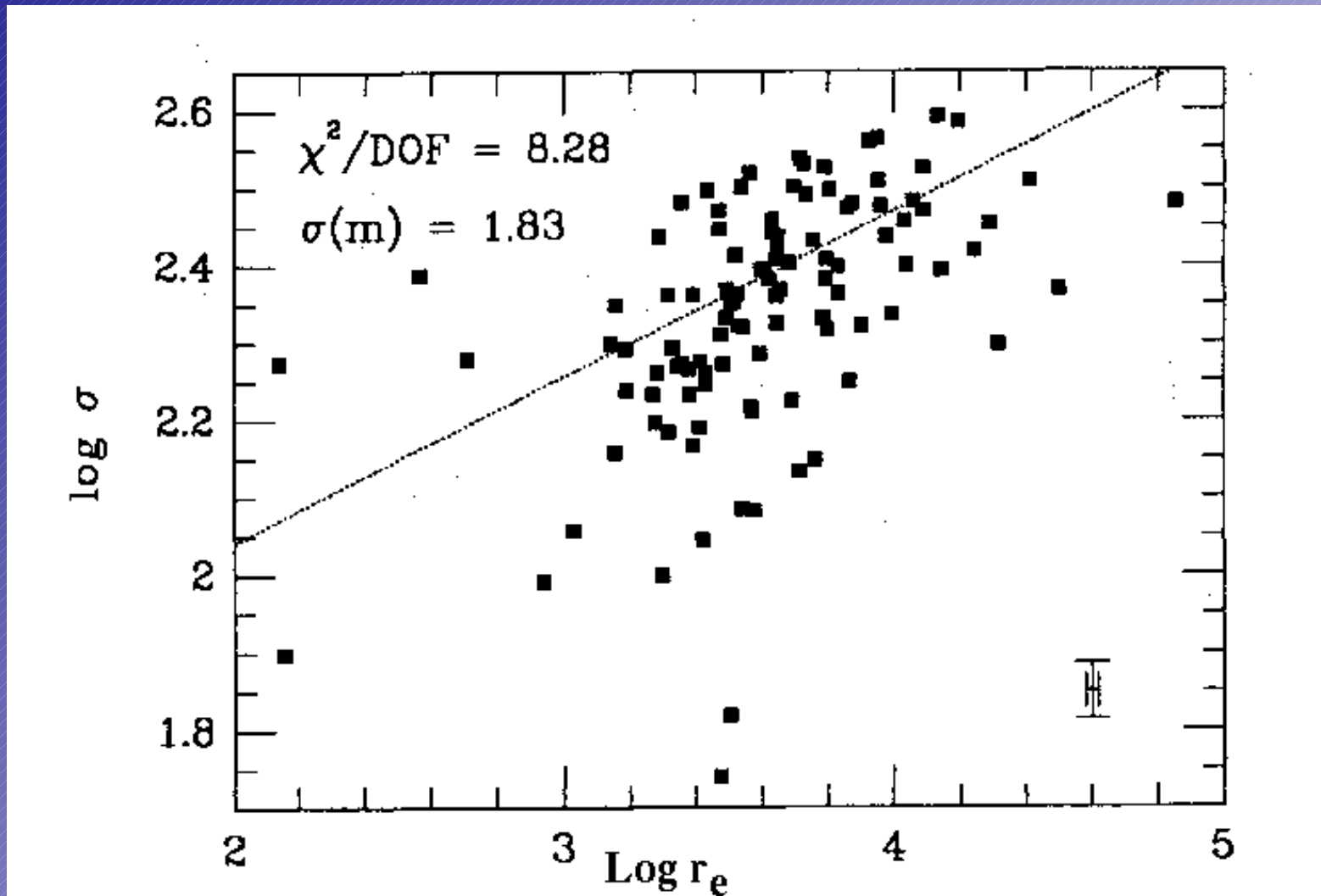
Characteristic	Boxy isophotes	Disky isophotes
Support	Mainly pressure	More rotational support
M/L ratio	Generally high with a wide range	Generally lower with a narrower range
Radio Luminosity	Brighter	Fainter
X-ray Luminosity	Brighter with a diffuse halo and discrete sources	Fainter with discrete sources dominate
Core	Frequent counter-rotating cores	Rarely have counter-rotating cores
Shape	Triaxial	Spheroidal



# Surface Brightness vs Luminosity



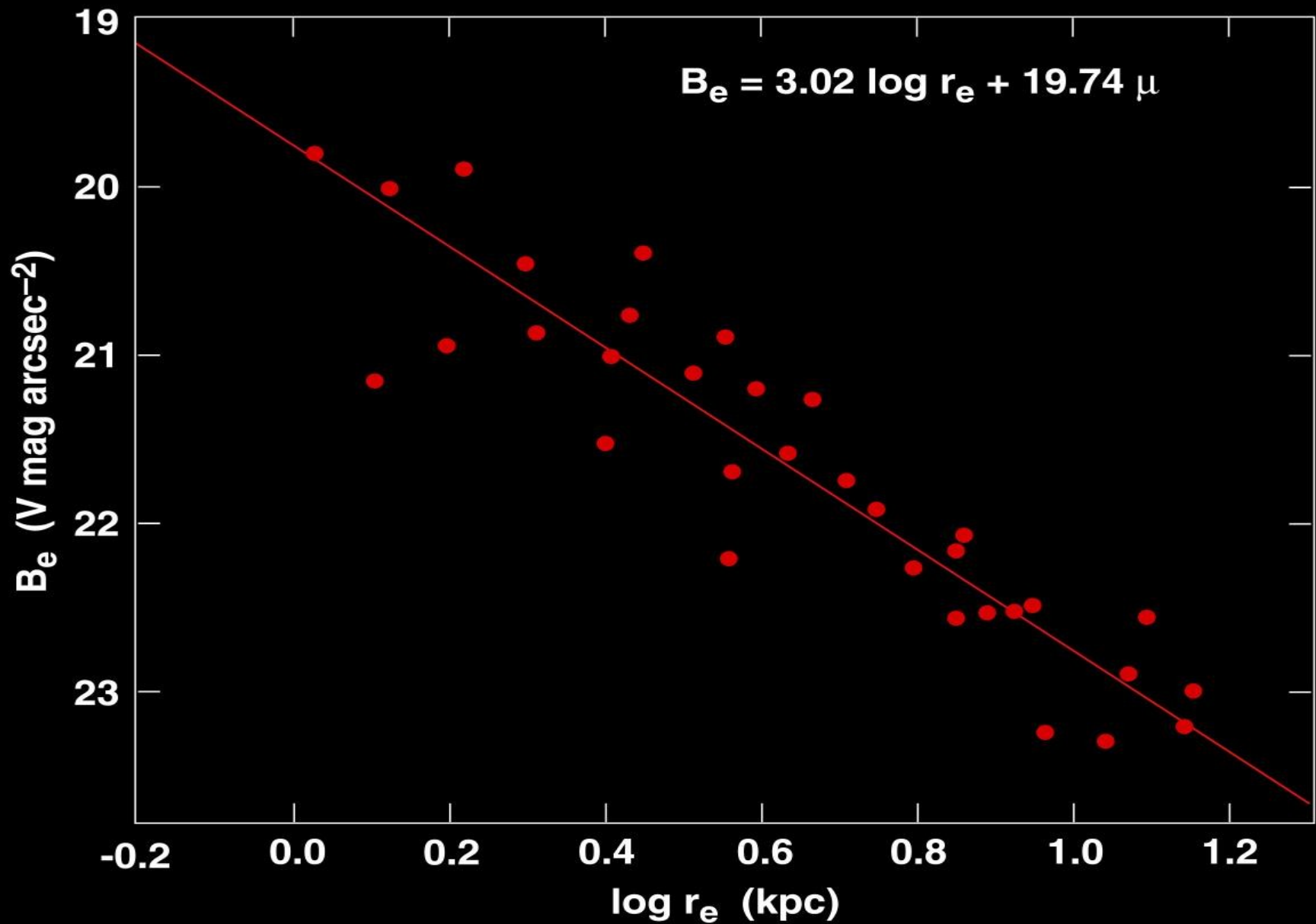
# $\sigma_r$ vs $R_e$



- In general, ellipticals --
  - Are supported by pressure (slow rotation), stellar motions are mostly random
  - Very little/no disk component
  - Very little/no star formation
  - Very little/no cold (e.g., HI) gas, but contains hot, X-ray gas
  - Almost exclusively found in high density environments (groups and clusters)
  - Populate a fundamental plane in luminosity-surface brightness-central velocity dispersion

# Elliptical Properties

- There are other correlations
  - Brighter ellipticals are bigger
  - Brighter ellipticals have lower average surface brightness
  - Can put these two together and form the Kormendy relation – larger galaxies have lower surface brightnesses:  
$$\Sigma_{B,e} = 3.02 \log r_e + 19.74$$
  - Brighter ellipticals have lower central surface brightness
  - Brighter ellipticals have larger core radii -- the core radius is the radius where the SB drops to  $\frac{1}{2}$  that of the central SB,  $I(r=0)$

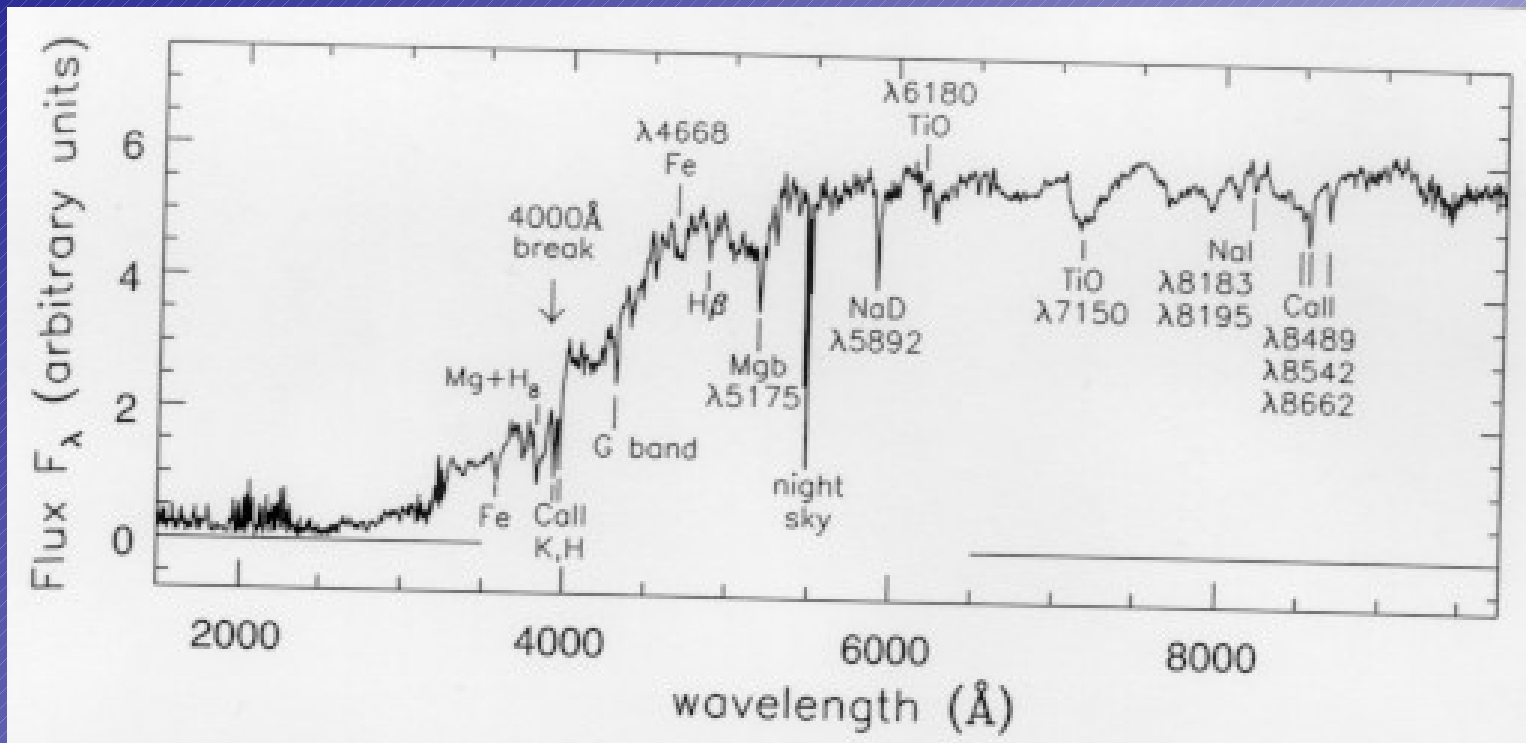


Kormendy (1977) relation

# What do the cores of ellipticals look like?

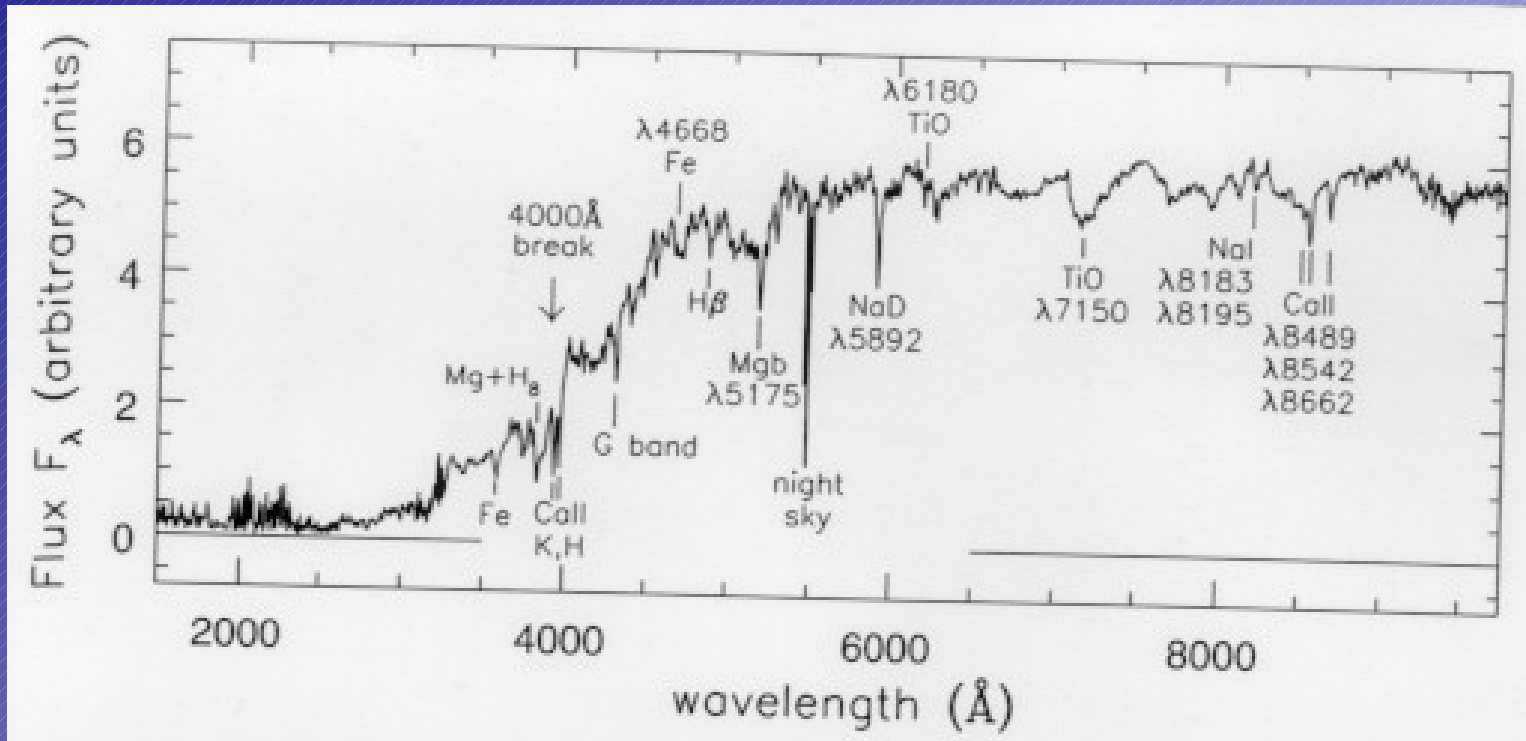
- The core of ellipticals is very hard to study because of atmospheric effects
- Not a problem with HST
  - Luminous ellipticals have power law cores
  - Moderate and dwarf ellipticals have central cusps

# Elliptical Spectrum



Note the lack of emission lines! The strong absorption lines are from metals. Metallicity in ellipticals are close to solar metallicity.

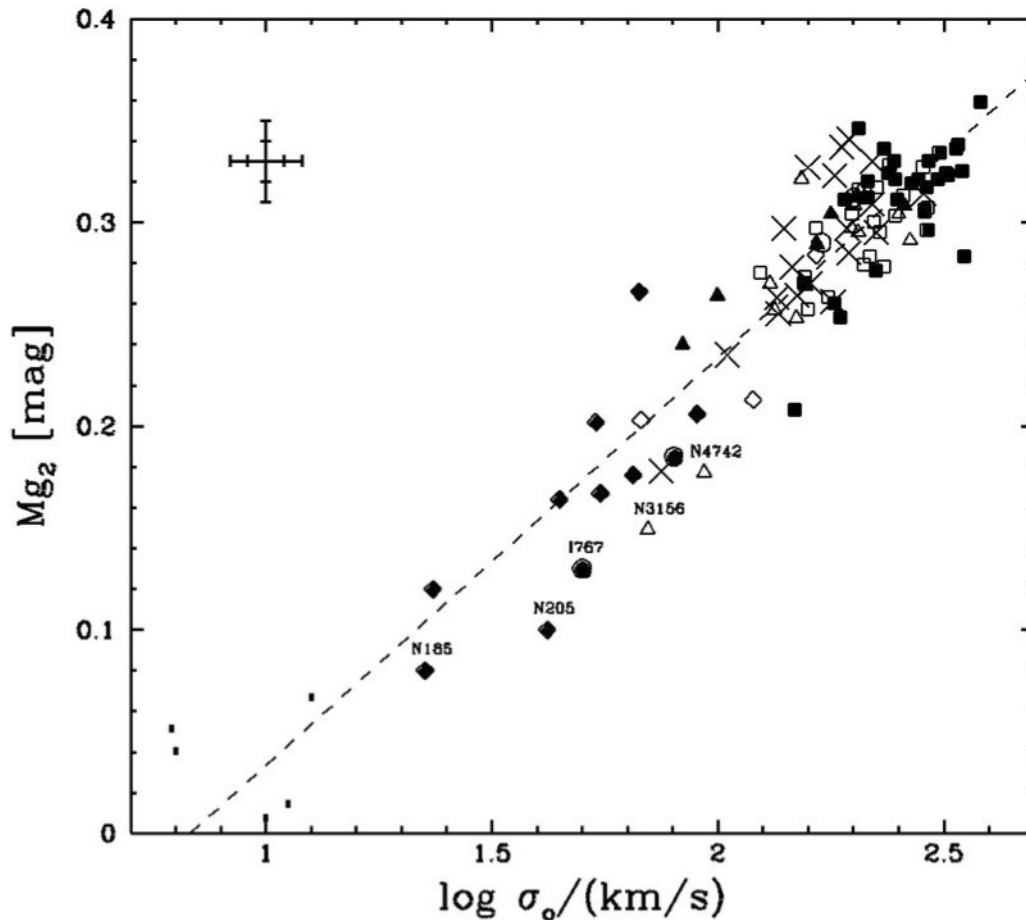
# Elliptical Spectrum



Note the lack of emission lines! The strong absorption lines are from metals. Metallicity in ellipticals are close to solar metallicity.



# Mg<sub>2</sub> vs $\sigma_0$



Bender IAU Symp 149  
Squares - ellipticals  
Crosses - S0 bulge  
Diamonds - dwarf  
Ellipticals  
Open squares -  
"special" objects

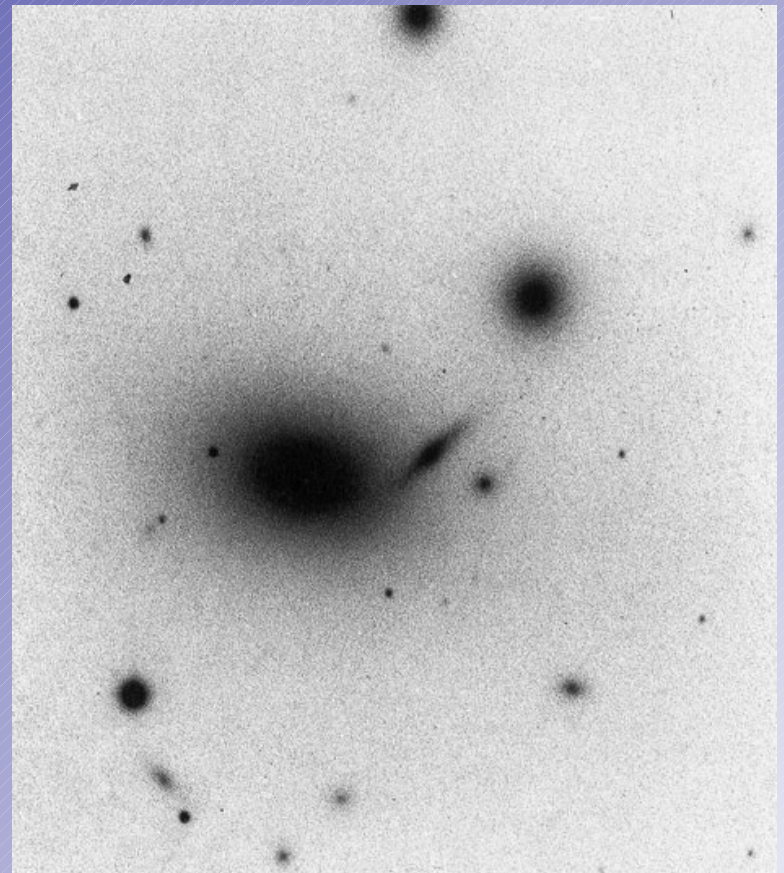
# Mg<sub>2</sub> vs $\sigma_0$ origin?

- Velocity dispersion is related to the depth of the potential well
  - $\sigma^2 \propto GM/R_e$
- Deeper potentials can
  - Hold on to more SNe enriched gas
  - Enriches the gas near the center of the potential
- Results in a higher stellar and gaseous metallicity

# Elliptical Galaxies



NGC 4552 (E0)



NGC 4889 (E4)

# Ellipticals cont.

- Traditional view
  - Ellipticals are simple and dull systems
    - Little or no gas or dust
    - Old stars
    - Form in a single collapse much like the GC simulation (violent relaxation)
    - Currently in equilibrium

# Ellipticals cont.

- We can roughly segregate E's by luminosity
  - Luminous:  $L > L_*$ ,  $M_B < -20$ ,  $L \approx 2 \times 10^{10} L_\odot$ ,
  - Midsized:  $L \sim (0.1-1.0)L_*$ ,  $M_B < -18$  to  $-20$ ,  
 $L \approx 3 \times 10^9 L_\odot$ ,
  - Dwarf:  $L < 0.1L_*$ ,  $M_B > -18$ ,  $L < 3 \times 10^9 L_\odot$ ,
- Unlike disk galaxies once you have measured the luminosity of an elliptical you can predict the other properties very accurately!

# Ellipticals cont.

- Luminosity profiles (1D):
  - Sersic profile:  $I(r) = I(r_e) \exp\{-b(r/r_e)^{1/n} - 1\}$
  - $r_e$  = effective radius which includes half the light (this defines the constant  $b$ ), and  $I(r_e)$  is the surface brightness at  $r_e$
  - Typical elliptical galaxies have  $n=4$ , or follow an  $r^{1/4}$ -law or “de Vaucouleurs’ law” ( de Vaucouleurs 1948)
    - $I(r) = I(r_e) \exp\{-7.67 (r/r_e)^{1/4} - 1\}$
  - provides good description for surface brightness of mid to bright ellipticals outside the center
  - cD galaxies have an “outer envelope” of extended light
- Ellipticals show 2D symmetry
  - Some have weak ripples, shells, other fine structure (remnants of mergers?)
  - Also boxy and/or disky isophotes

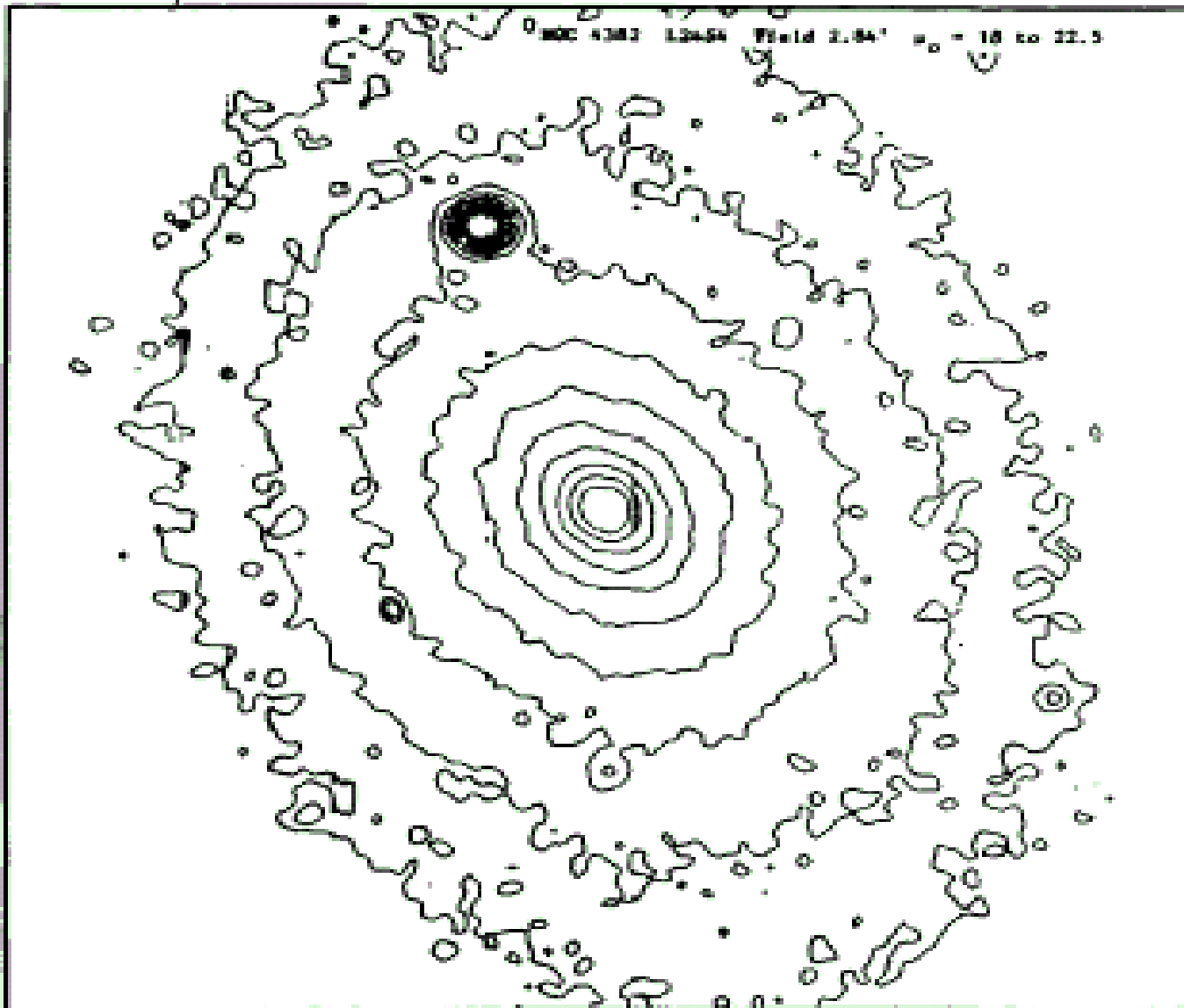
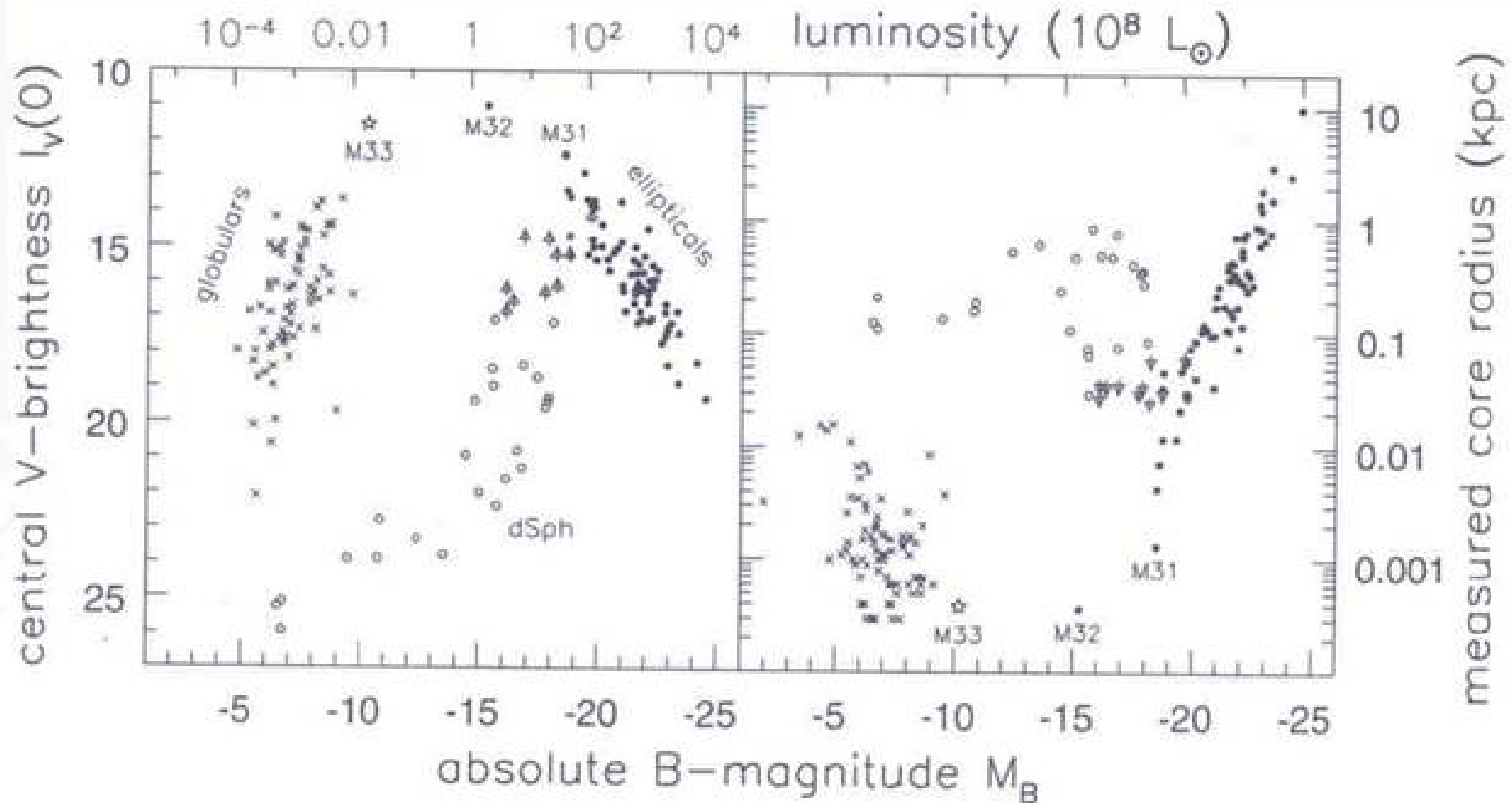


FIGURE 5.5.

Michard 1985



**Figure 6.6** Central surface brightness  $I_V(0)$  in  $\text{mag arcsec}^{-2}$  in the V band, and core radius  $r_c$ , measured from the ground, plotted against B-band luminosity  $M_B$ . Filled circles are elliptical galaxies and bulges of spirals (including the Andromeda galaxy M31); open circles are dwarf spheroidals; crosses are globular clusters; the star is the nucleus of Sc galaxy M33. Arrows show ellipticals in the Virgo cluster; here, seeing may cause us to measure too low a central brightness, and too large a core – J. Kormendy.



If  $q$  is the ratio of the minor to the major axis then

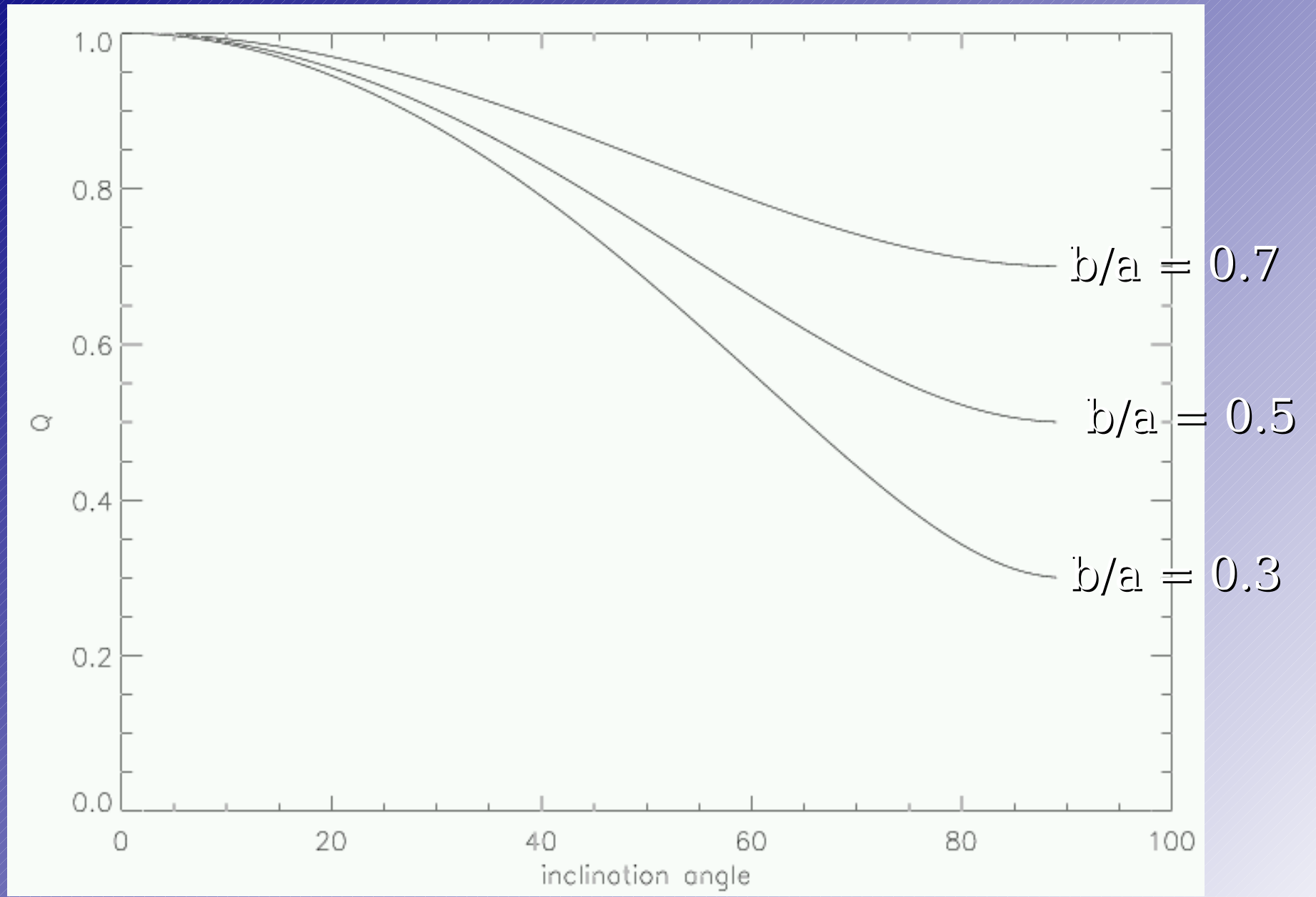
$$q_{obl} = \frac{b}{a} = OQ \frac{\sin(i)}{mA} = \frac{B^2 m}{zA} \sin(i) = \left[ \frac{B^2}{A^2} + \cot^2(i) \right]^{1/2} \sin(i)$$

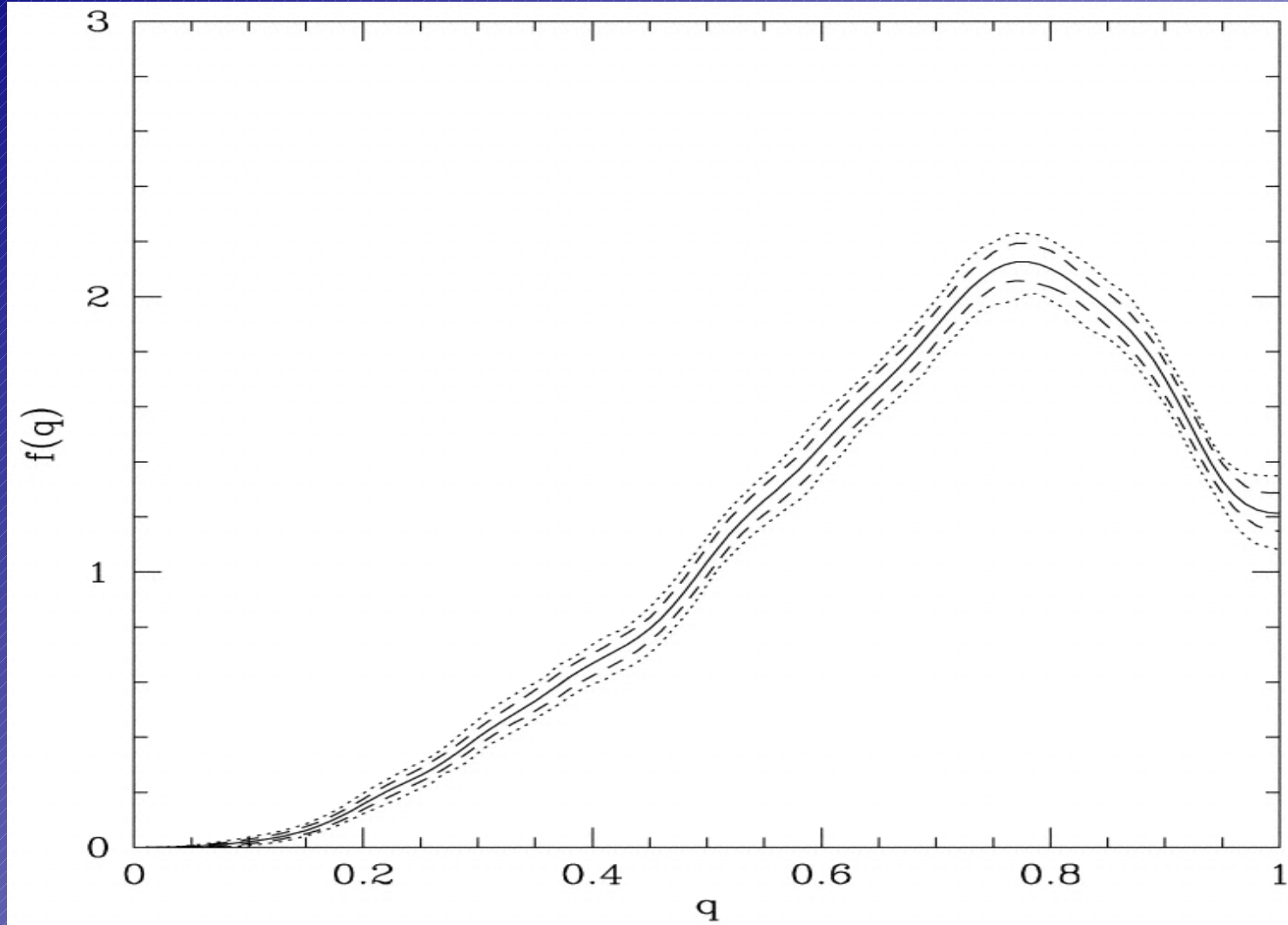
Using our definition of  $m$  for the last step. Finally we can rewrite this as

$$q_{obl}^2 = (b/a)^2 = (B/A)^2 \sin^2(i) + \cos^2(i)$$

For an oblate spheroid we can do all this again and get

$$q_{prol}^2 = (b/a)^2 = \left[ (B/A)^2 \sin^2(i) + \cos^2(i) \right]^{-1}$$

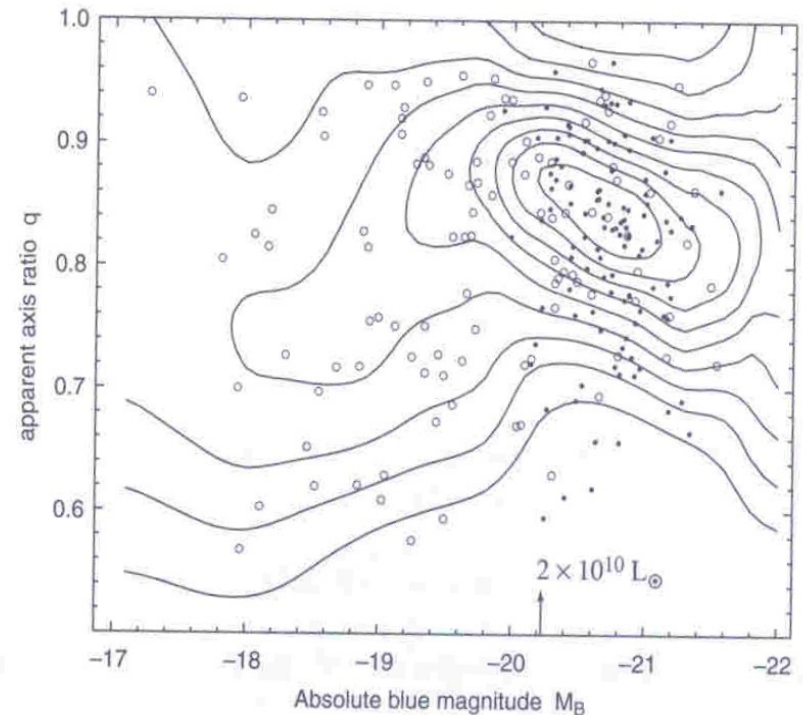




Axial ratios for galaxies fit with de Vaucouleurs profiles (Khairul Alam & Ryden 2002).

# Distribution of B/A cont.

- Small E's are more elongated than more luminous E's
- Midsized E's have  $q \approx 0.75$
- Luminous E's have  $q \approx 0.85$ 
  - No selection of oblate spheroids can give the observed distribution
  - These galaxies must be triaxial



**Figure 6.9** Observed axis ratio  $q$  and blue absolute magnitude  $M_B$  for elliptical galaxies from two different samples, represented by filled and open circles. Bright galaxies (on the right) on average appear rounder. Contours show probability density; the top contour level is 4.5 times higher than at the lowest, with others equally spaced – B. Tremblay & D. Merritt, AJ 111, 2243; 1996.

- Deviations from ellipses can be disky or boxy
- Measure difference between observed isophote and fitted ellipse as:
  - $\Delta r(\theta) = \sum_{k=3} a_k \cos(k\theta) + b_k \sin(k\theta)$
  - $\theta$  = angle around ellipse,  $\Delta r(\theta)$  is distance between fitted ellipse and observed isophote
  - $a_3$  and  $b_3$  describe “egg-shaped” ellipses, generally small,  $b_4$  is also usually small
  - $a_4 > 0$ , isophote is disky (extra light along the axis)
  - $a_4 < 0$  isophote is boxy (extra light at the corners)

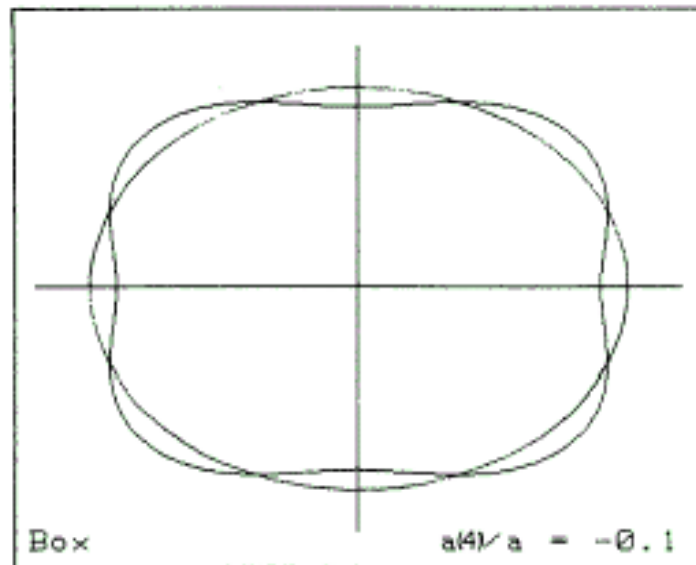
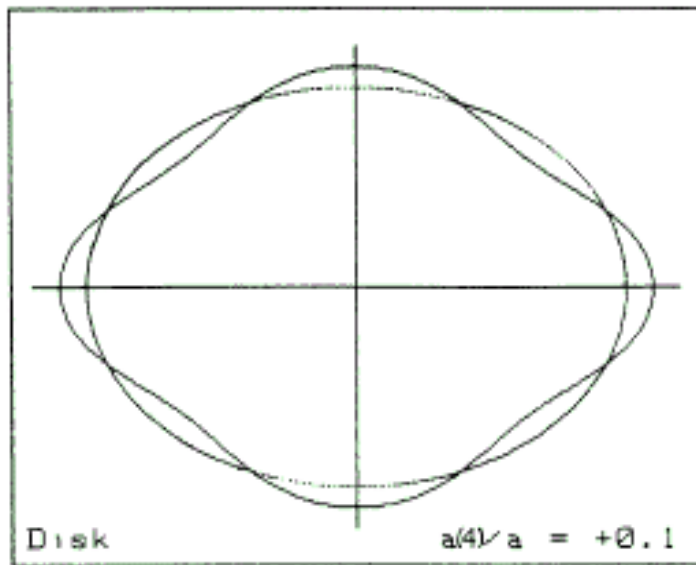


FIGURE 5. — Schematic drawing illustrating isophotes with  $a(4)/a = +0.1$  and  $a(4)/a = -0.1$ .

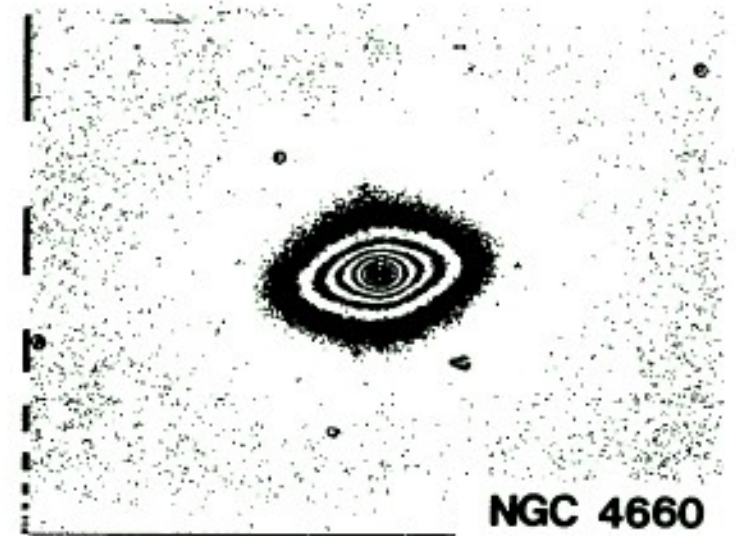


FIGURE 6. — R-image of NGC 4660, an elliptical galaxy with a disk-component in the isophotes ( $a(4)/a \sim +0.03$ ).

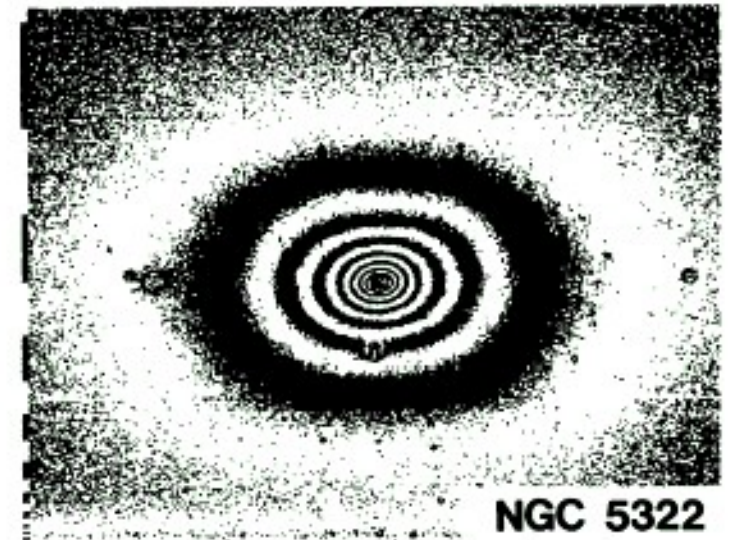
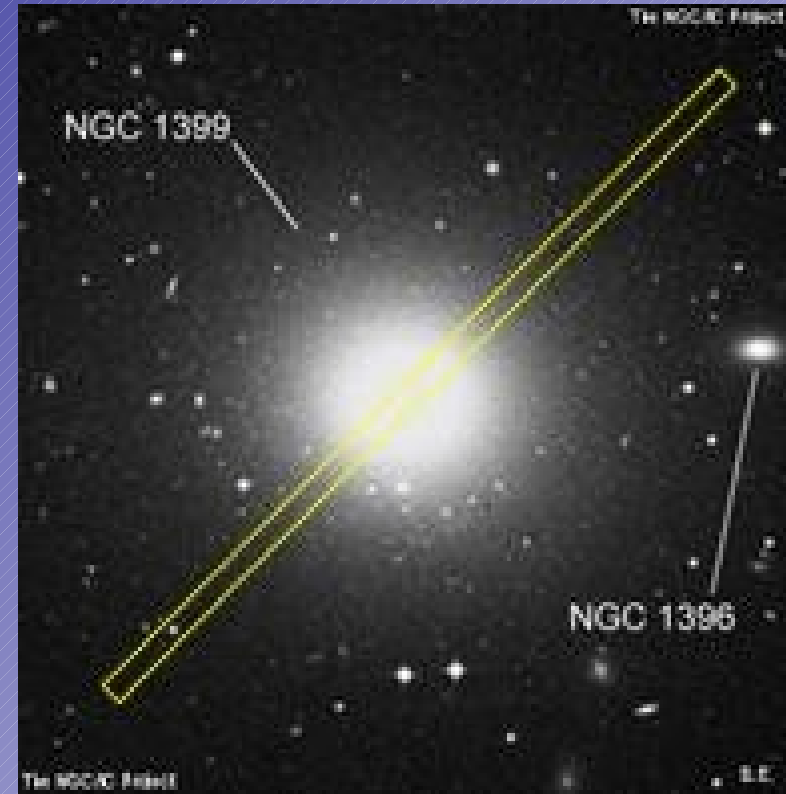
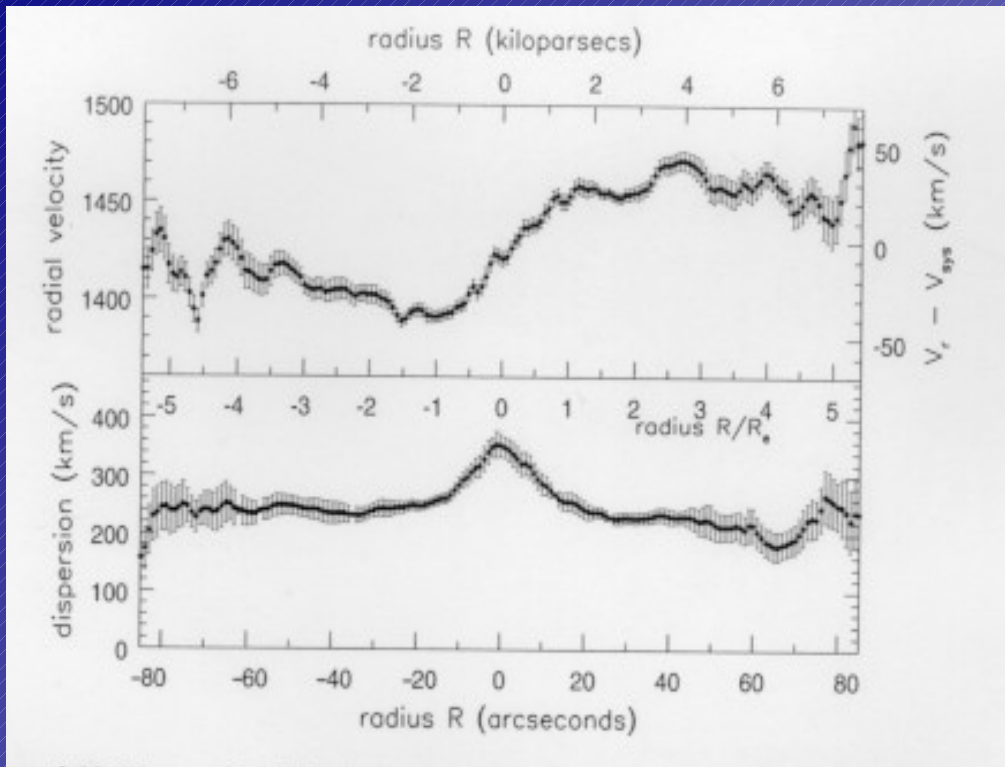


FIGURE 7. — R-image of NGC 5322, an elliptical galaxy with box-shaped isophotes ( $a(4)/a \sim -0.01$ ).

# Some ellipticals are just different





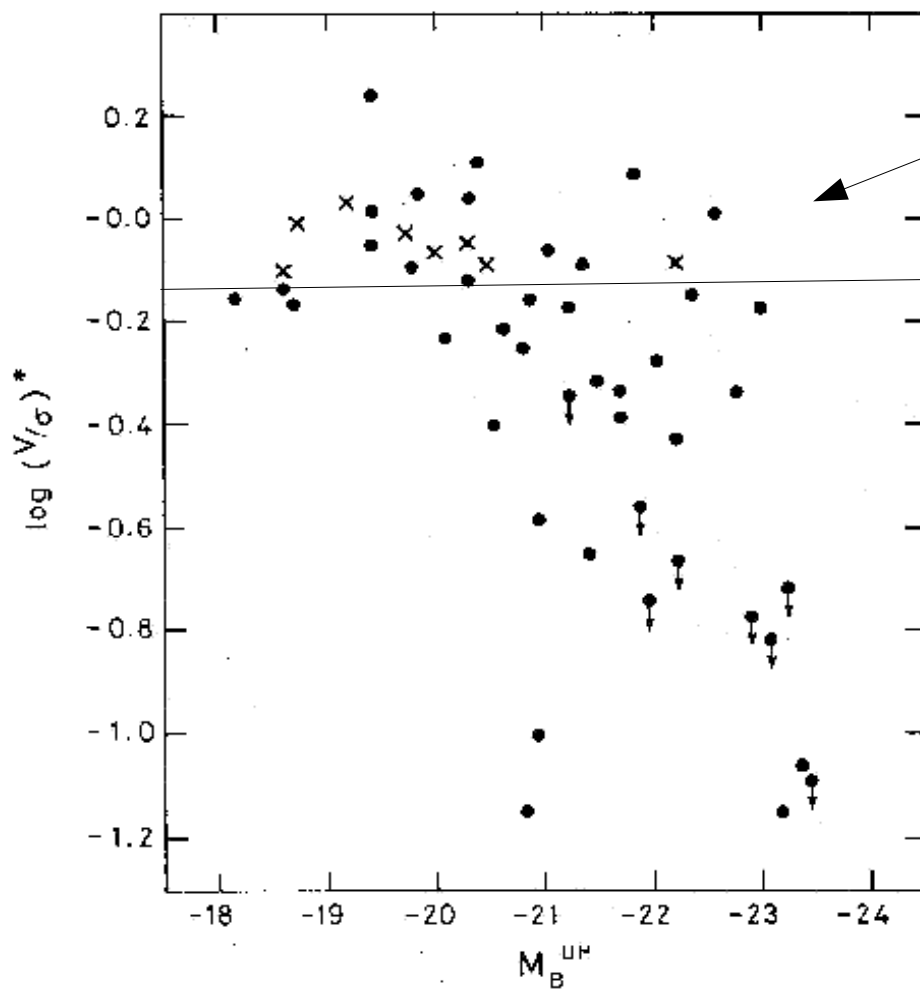
To measure the rotation of elliptical galaxies cannot use HI or emission lines. So we place a long slit spectrograph (same as for spirals) and measure the absorption lines in the stellar spectra.



# Kinematics of Ellipticals cont.

- Rotation implies that ellipticals are not relaxed systems
  - Some have kinematically decoupled cores, or rotation along their minor axis (implies triaxiality)

# $V_{\text{rot}}/\sigma$ vs Luminosity



Rotationally supported

Rotational Properties  
of Elliptical Galaxies:

**Anisotropy parameter:**

$$\left(\frac{v}{\sigma}\right)^* \equiv \frac{v/\sigma}{\sqrt{\frac{1-b/a}{b/a}}} = \frac{(v/\sigma)_{\text{observed}}}{(v/\sigma)_{\text{rot. flattened}}}$$

see: Davies et al. (1983)  
*ApJ*, **266**, 41

FIG. 4.—Log  $(V/\sigma)^*$  against absolute magnitude. Ellipticals are shown as filled circles and the bulges as crosses;  $(V/\sigma)^*$  is defined in § IIIb.

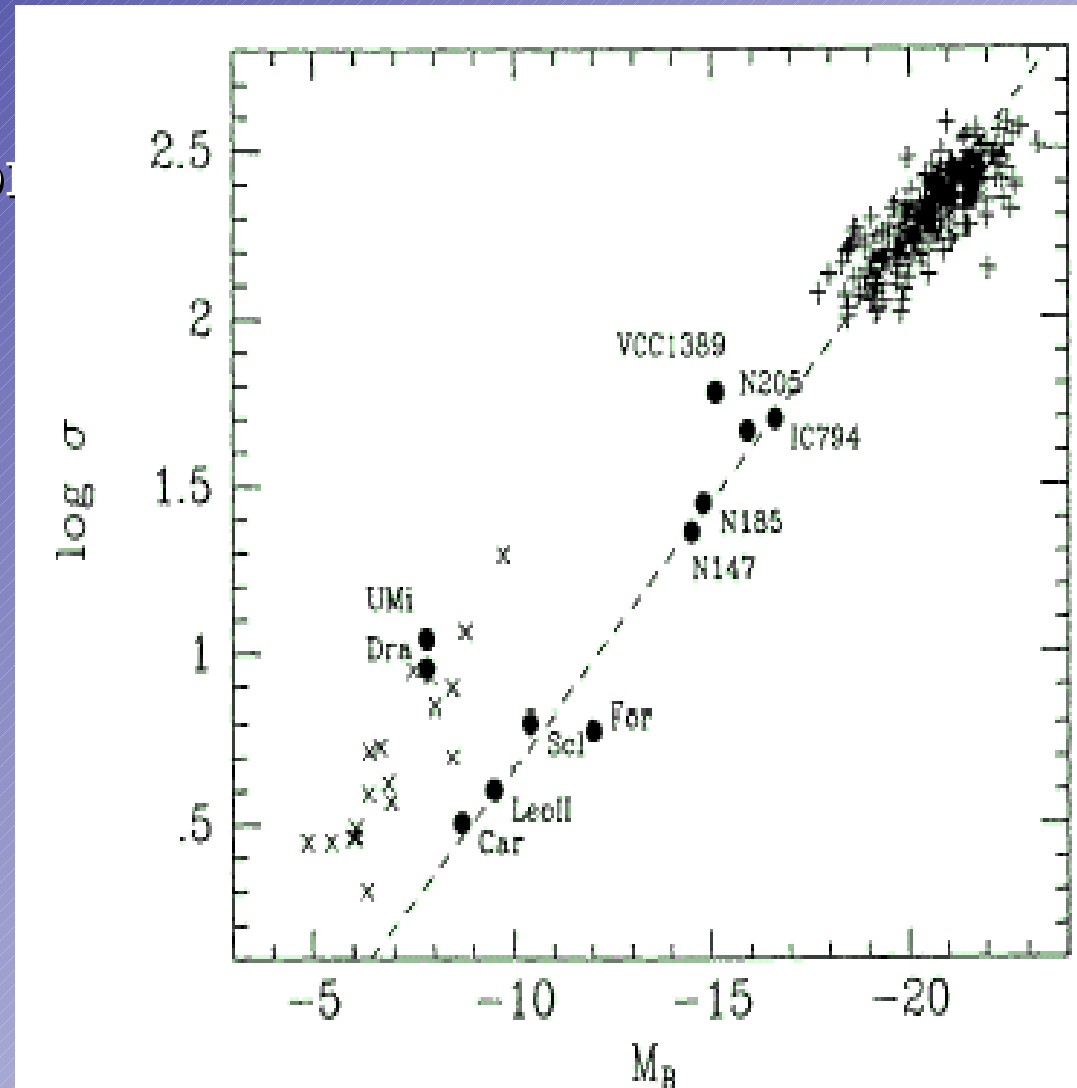
# Faber-Jackson Relation

- Faber & Jackson(1976) found that:
  - Roughly,  $L \propto \sigma^4$ 
    - More luminous galaxies have deeper potentials
  - Can show that this follows from the Virial Theorem (just like Tully-Fisher relation)

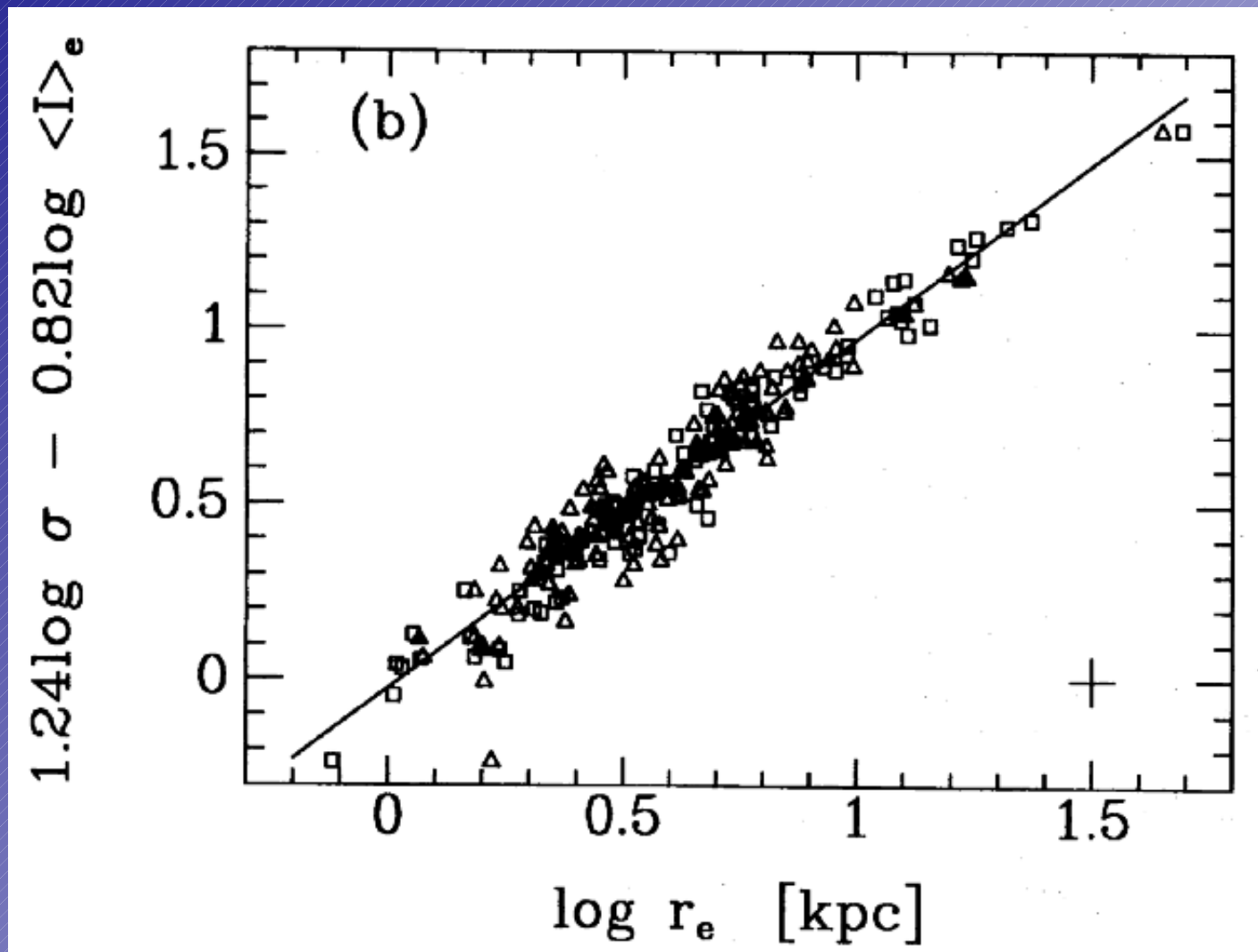
# Faber-Jackson relation cont.

- This is similar to the Tully-Fisher relation for Spirals
- Used to measure distance from  $\sigma$
- Problem:
  - E's have very extended halos so getting the total luminosity is tricky

$$\frac{L_v}{2 \times 10^{10} L_{sun}} \approx \left( \frac{\sigma}{200 \text{ km s}^{-1}} \right)^4$$



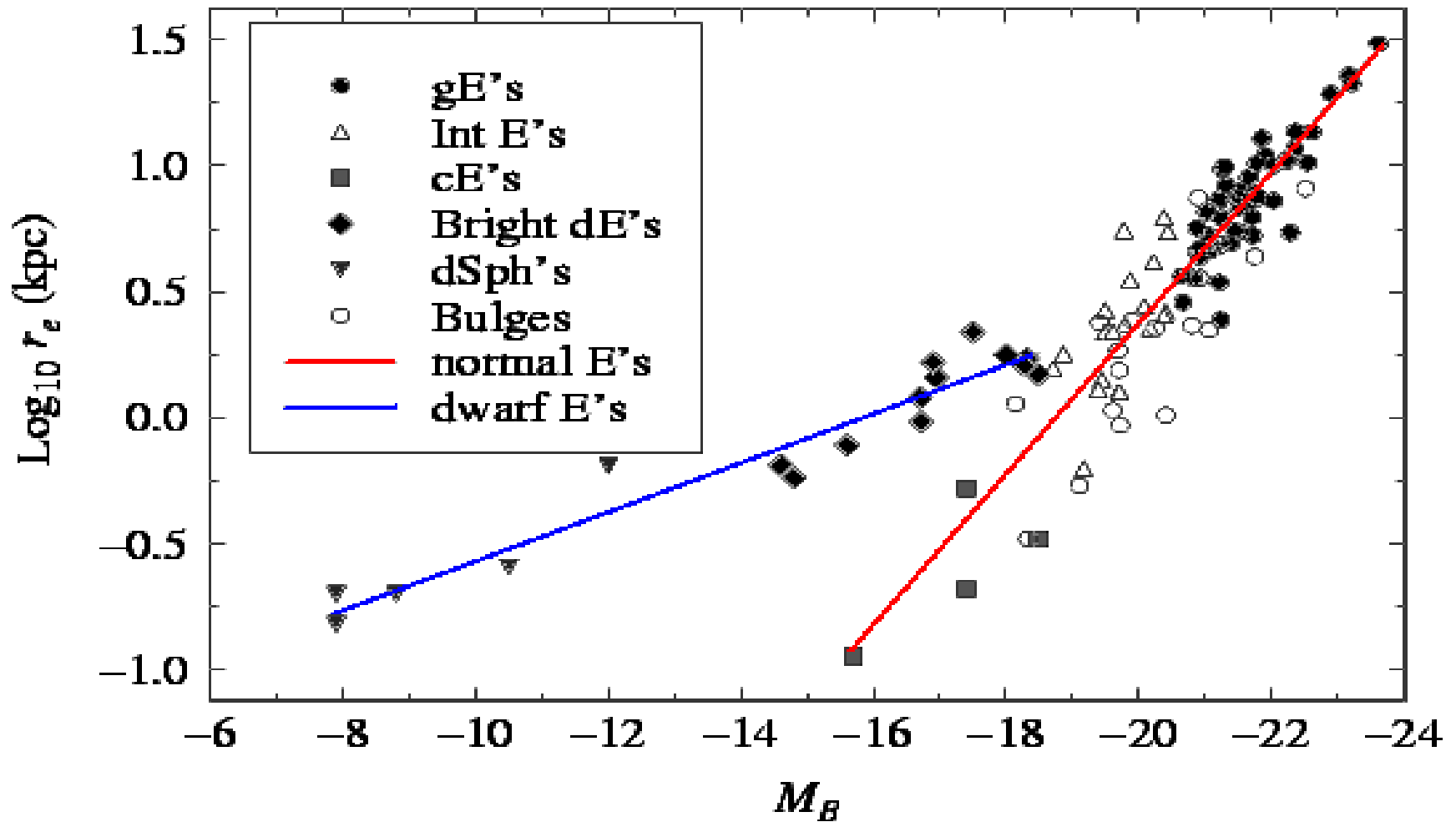
# Fundamental Plane



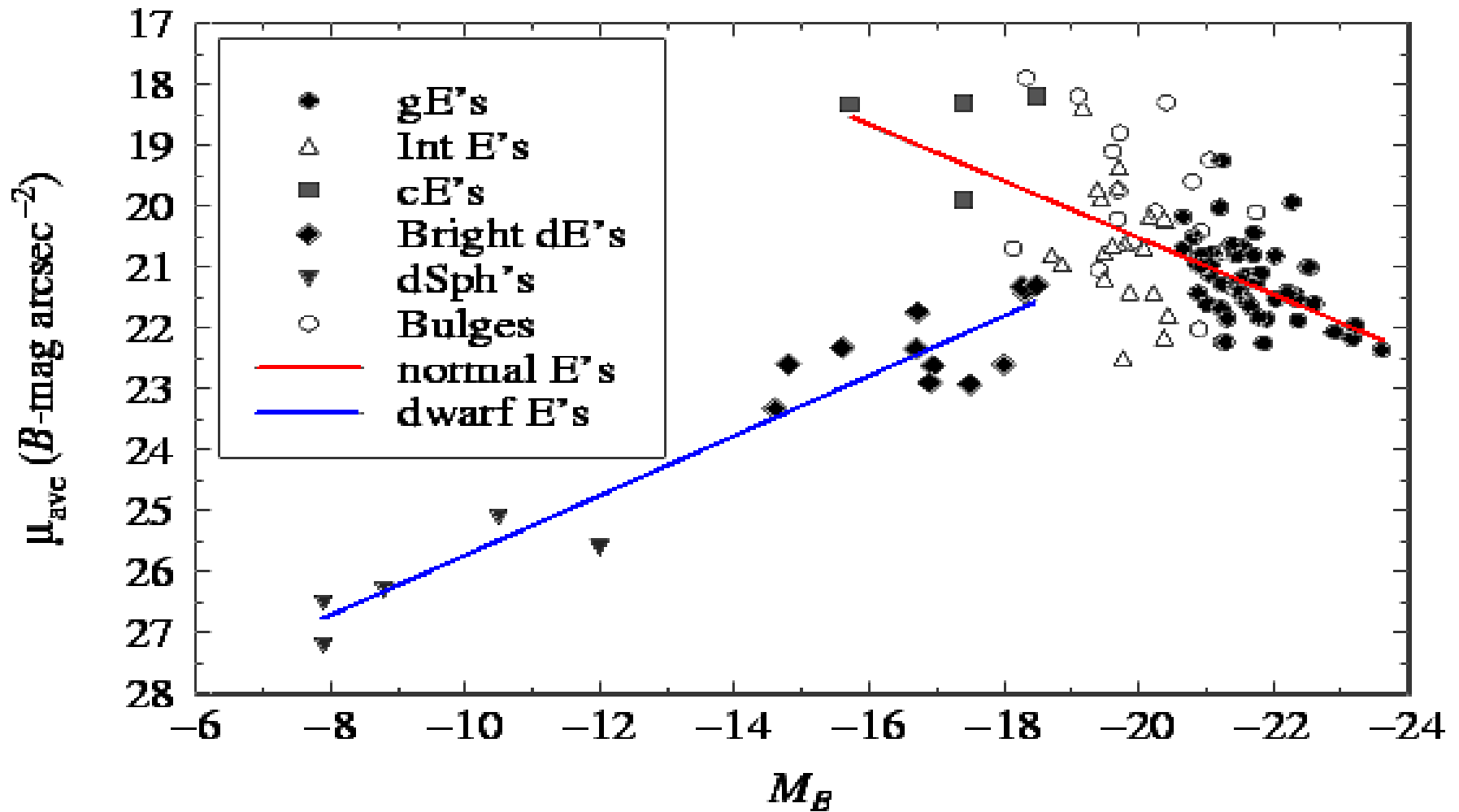
# Fundamental Plane

- Observers found that if you plotted
  - $R_e$
  - $I(R_e)$  and the
  - central  $\sigma$
- These quantities define a plane – the “Fundamental Plane”
- $R_e \propto \sigma^{1.24} I_e^{-0.82}$
- This, like the Tully-Fisher relationship, reflects some fundamental physics for formation of ellipticals!

# Effective radius vs $M_B$



# $\langle \Sigma \rangle$ vs $M_B$





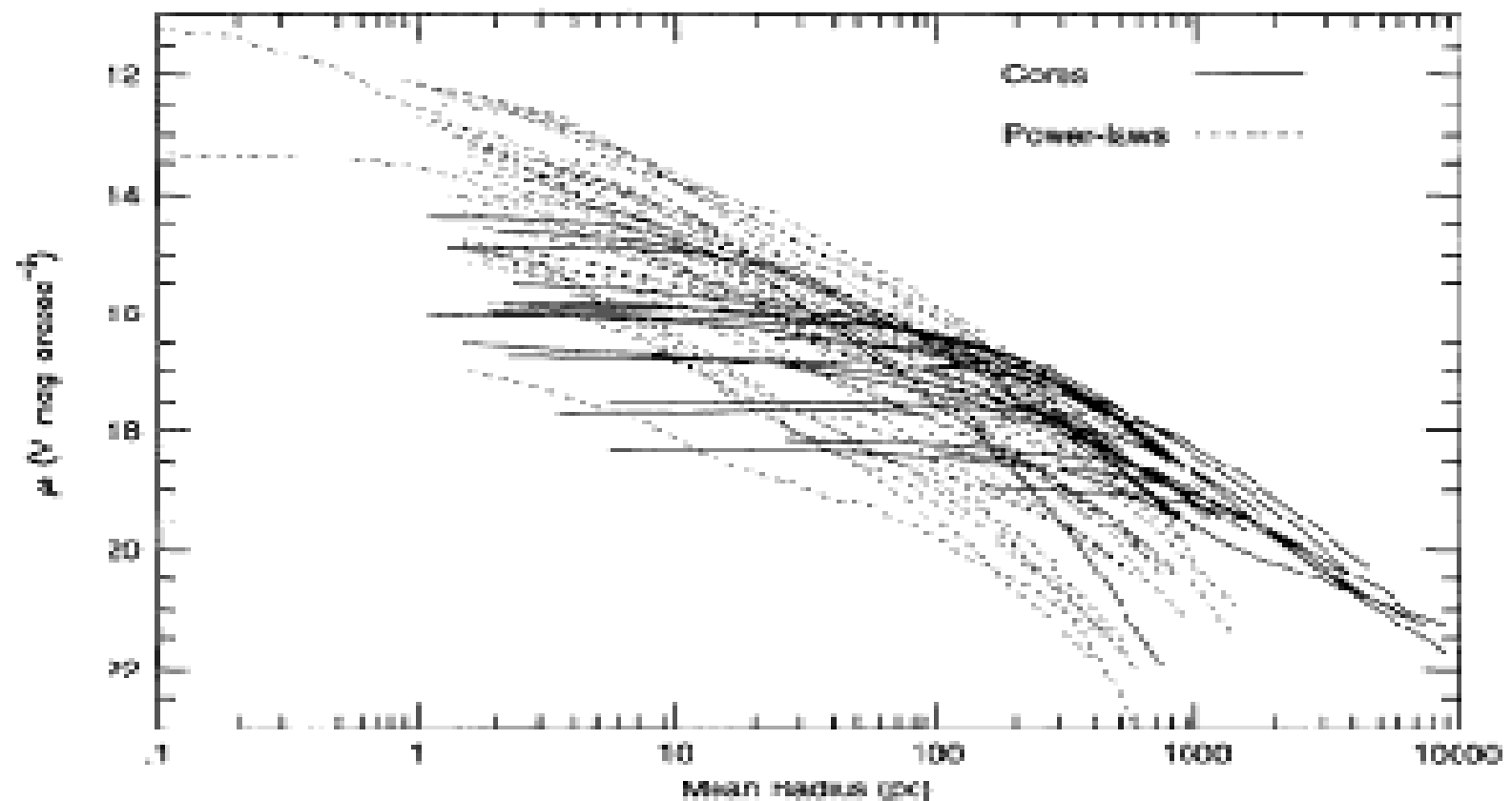


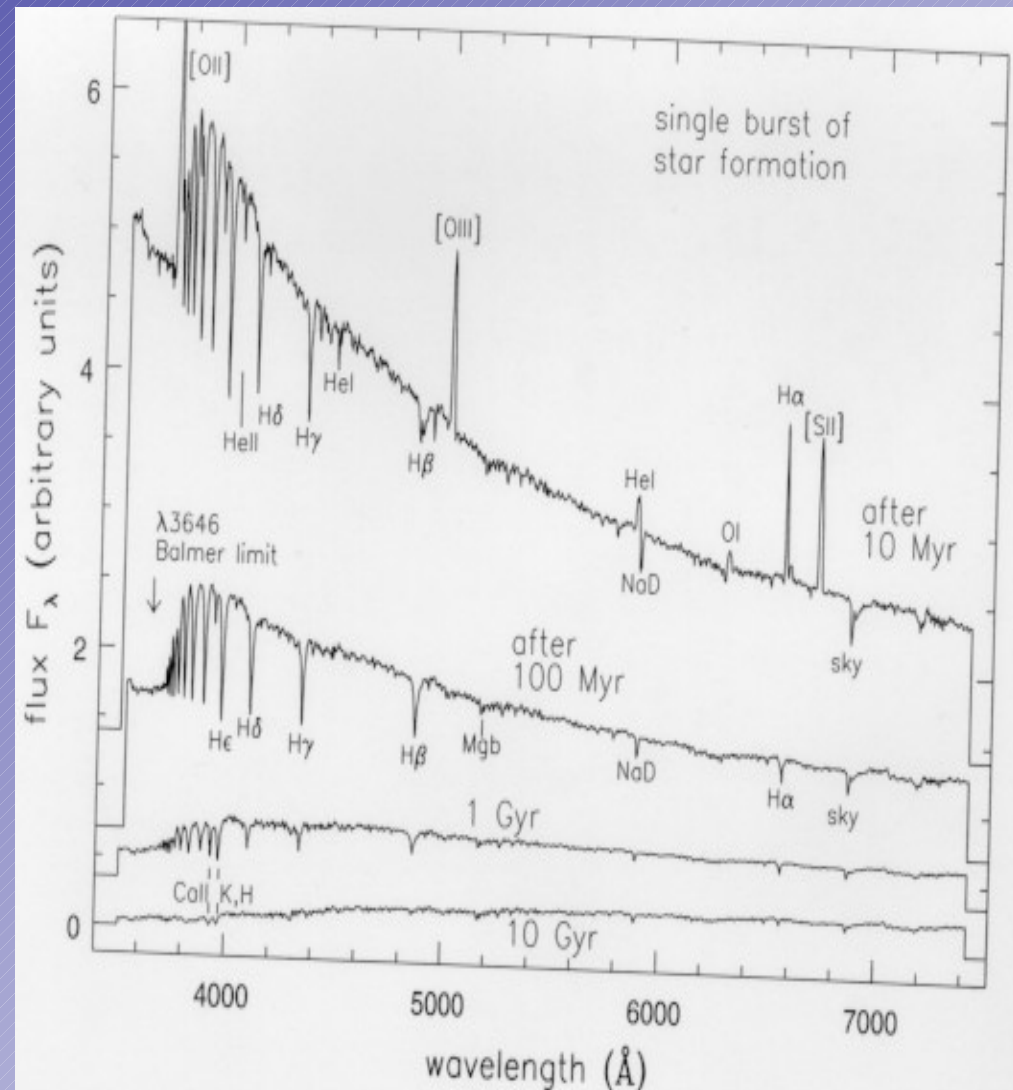
FIG. 1.  $V$ -band surface-brightness profiles of 55 ellipticals and bulges from *HST*. All were observed in the WFPC1 Planetary Camera through filter F555W and were deconvolved using the Lucy-Richardson algorithm as described in Paper I. Core galaxies (see Sec. 2) are plotted as solid lines, and power-law galaxies are plotted as dashed lines. “Mean radius” is the geometric mean of the semimajor and semiminor axes of the isophotal ellipse.

# Stellar Populations

- Ellipticals are full of old, red stars
- Ellipticals follow a color-magnitude relation such that more luminous galaxies are redder
  - Is this due to age or metallicity?
- This is known as the age/metallicity degeneracy!!

# Starburst Spectra

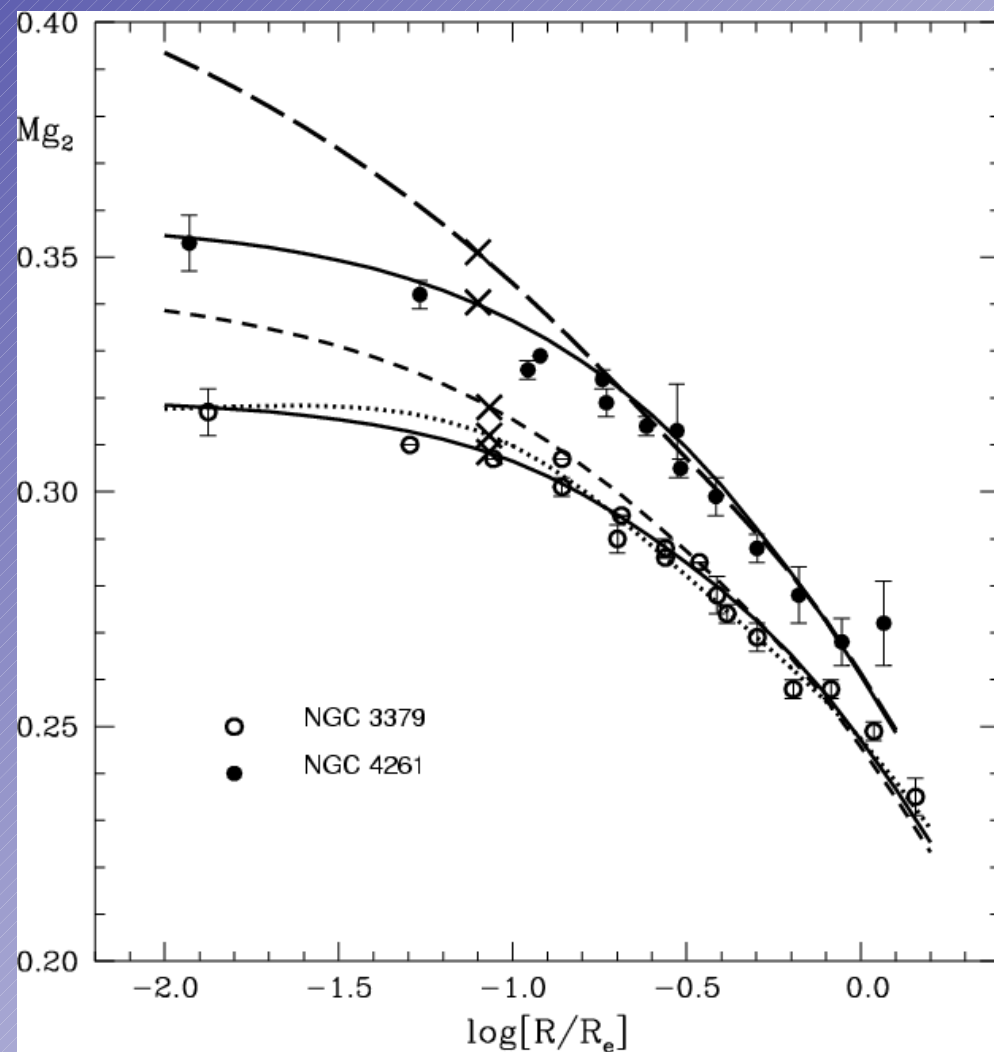
- If smaller ellipticals are younger then they should be bluer
  - A young starburst has a very blue spectrum
  - As the population ages it becomes redder and we see lots of A stars (E+A galaxies)
  - After  $2 \times 10^9$  yrs we see a spectrum similar to ellipticals today



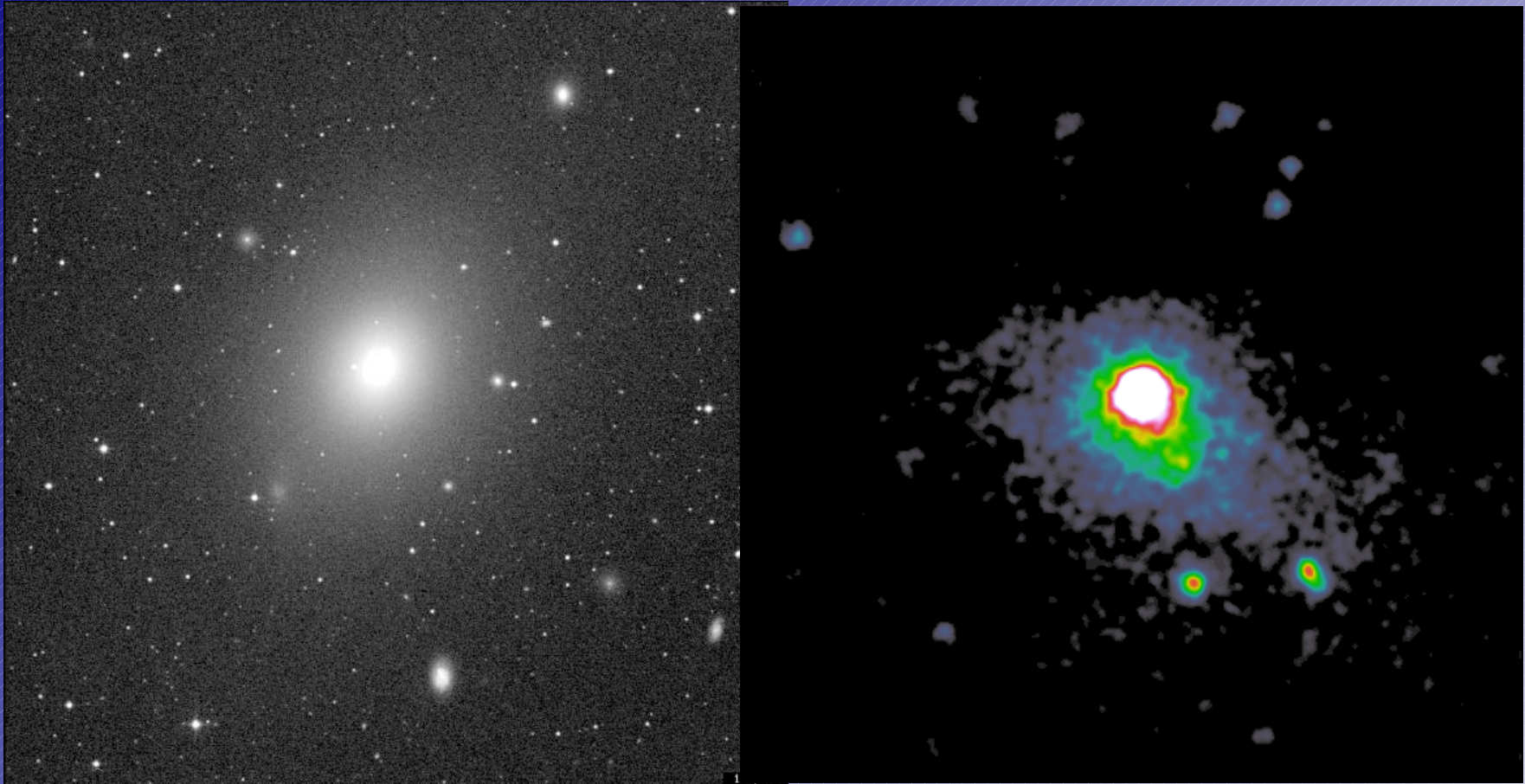
# Metallicity

- Can also be a metallicity effect
  - Lower metallicity
  - Less absorption in the blue part of the spectrum
  - Bluer galaxy
- Why would smaller galaxies have less metals
  - Less luminosity --> less mass
  - SNe explosions --> high speed gas
  - So less massive galaxies are less effective at retaining metal rich gas
  - This would lead to a trend that smaller ellipticals would be bluer!

# Abundance Gradients



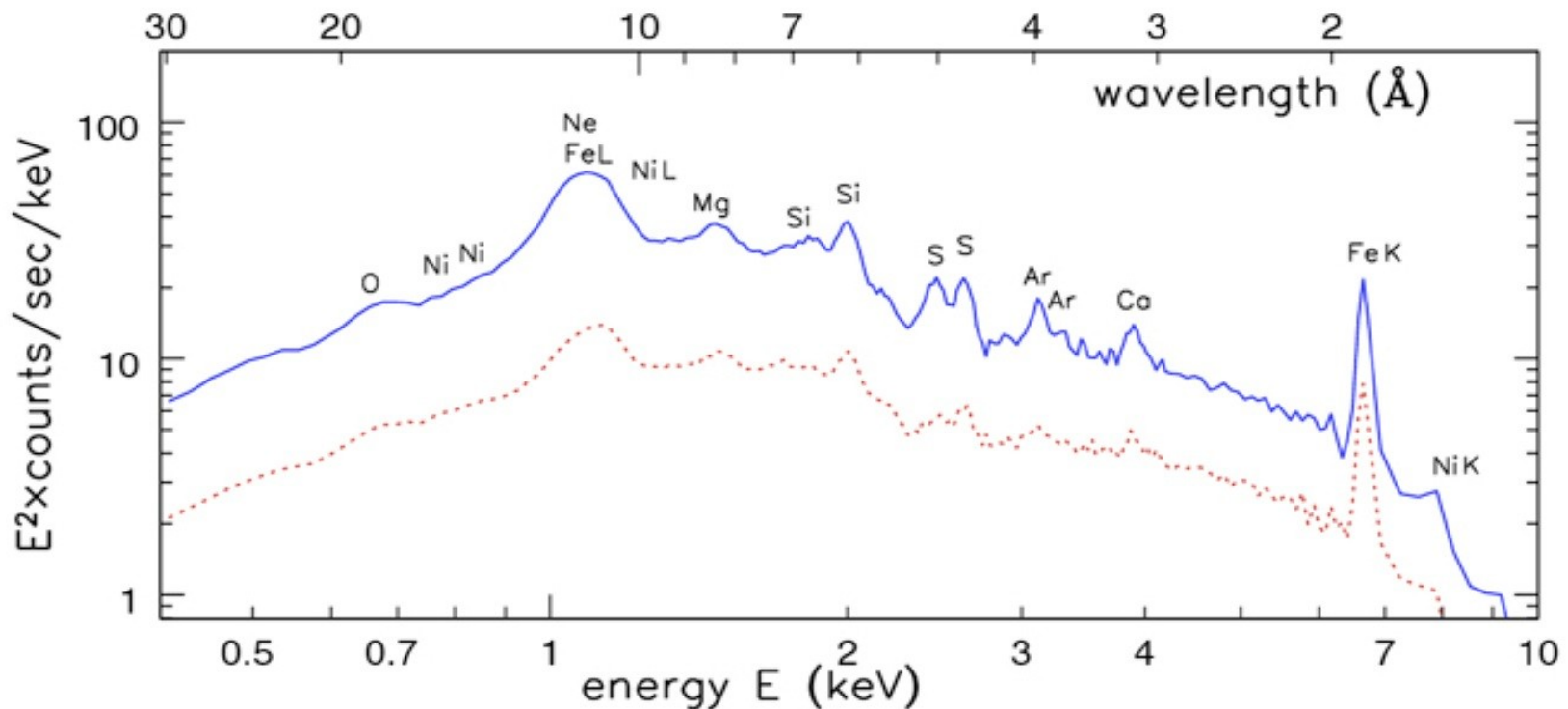
# X-ray Halos



Optical and X-ray images of M49

# X-ray Halos cont.

- Where does the hot gas come from ?
  - We know that it is metal rich ( $Z \sim 0.5$  solar)



# X-ray Halos cont.

- Where does the hot gas come from ?
  - Stellar winds from red giants and red supergiants
    - Random velocities  $\geq 350$  km/s and we know that  $(1/2)m\sigma^2 \sim 3/2 kT$
    - So when the stellar winds collide it heats the gas to  $> 10^6$  K
- The mass of hot gas can be from  $10^8 - 10^{11} M_{\odot}$



# X-ray Halos cont.

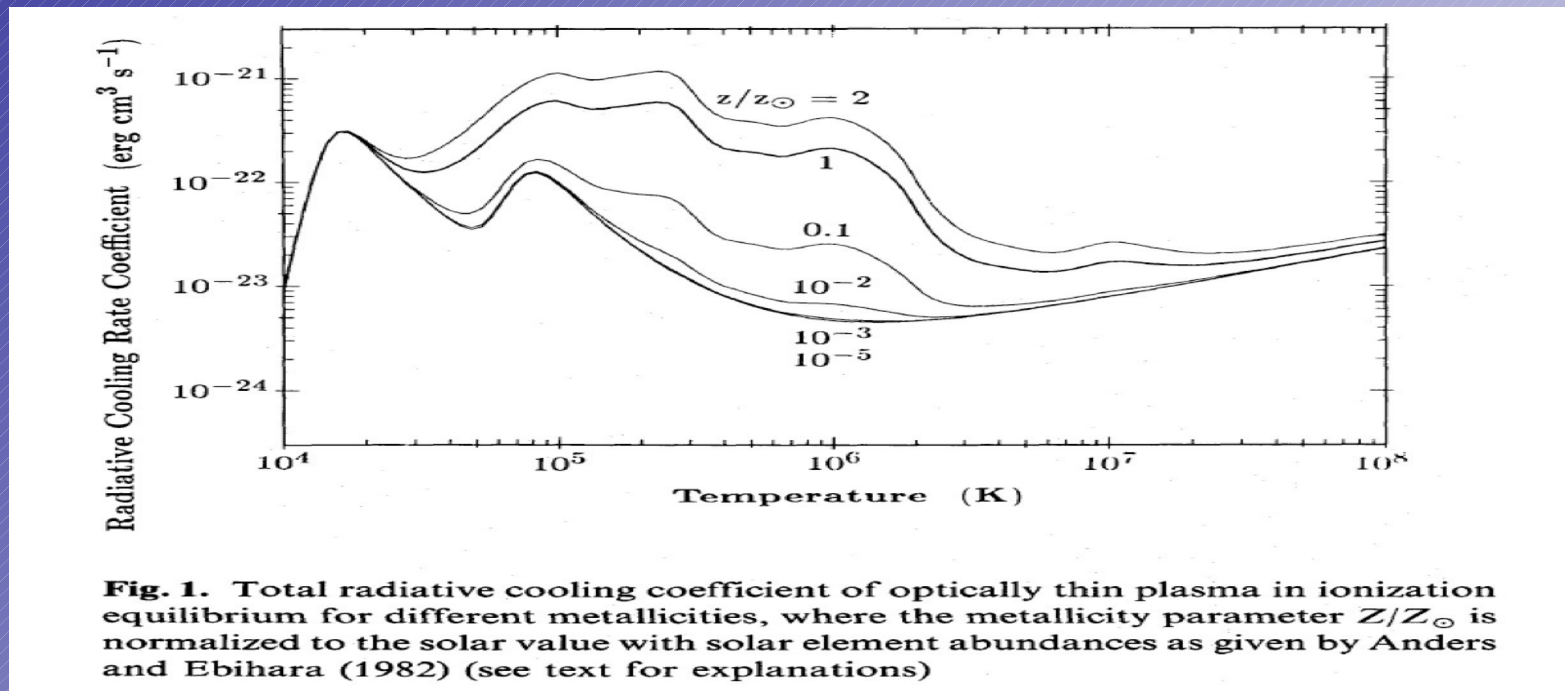
- We see lines from “metals”
  - So at least some of this gas is processed by stars and injected into the ISM via SNe.
  - Typical values are from 0.2 – 0.8 solar
  - SNe produce ejecta enriched 2-5x solar
  - So how do we get gas with less metals?

# X-ray Halos cont.

- So how do we get gas with less metals?
  - Dilution
  - Stellar winds
  - Combination

# X-ray Halos cont.

- X-ray emission is a major source of cooling the X-ray gas
  - M87 emits  $\sim 3 \times 10^{42}$  erg/s



**Fig. 1.** Total radiative cooling coefficient of optically thin plasma in ionization equilibrium for different metallicities, where the metallicity parameter  $Z/Z_{\odot}$  is normalized to the solar value with solar element abundances as given by Anders and Ebihara (1982) (see text for explanations)

# X-ray Halos cont.

- How fast does does the gas cool?

$$t_{\text{cool}} = kT^{1/2} / 2 \times 10^{-27} n_e$$
$$= 2.2 \times 10^{10} \text{ yr } (T/10^8 \text{ K})^{1/2} (n_e/10^{-3} \text{ cm}^{-3})^{-1}$$

This is larger than the Hubble time so elliptical galaxies will not cool much!

# X-ray Halos cont.

- How fast can the gas reach equilibrium?

The timescale for the gas to relax is just

$$t_{\text{relax}} = d/c_s$$

The sound speed in a gas is just

$$c_s = (\gamma P/\rho)^{1/2}$$

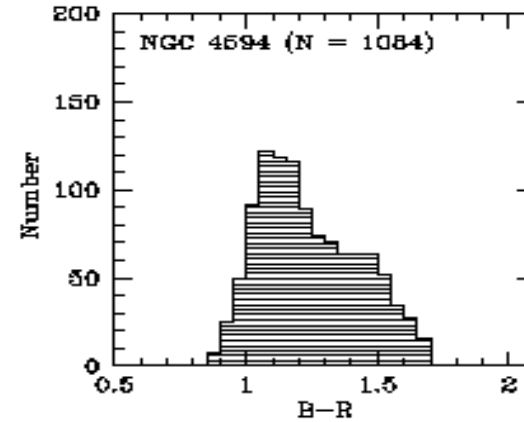
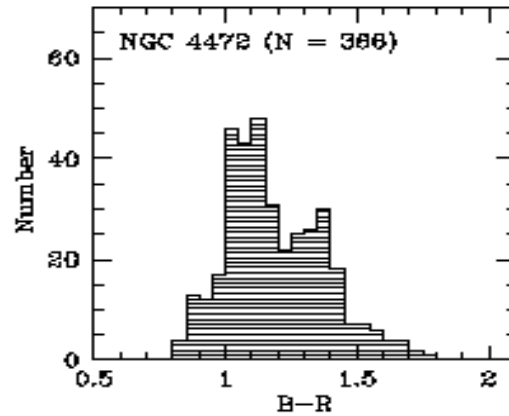
$$= 6.5 \times 10^8 \text{ yr } (T/10^8 \text{ K})^{-1/2} (d/\text{Mpc})$$

This is much smaller than the Hubble time so the hot gas is almost always in equilibrium!

# Globular Clusters in Ellipticals

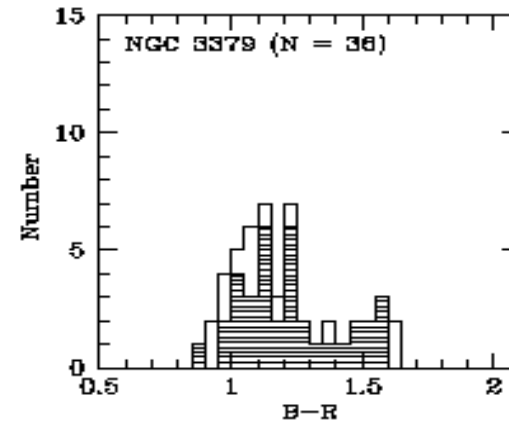
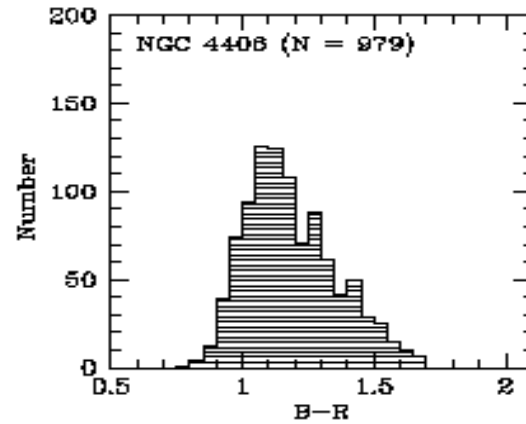
- Ellipticals are surrounded by a halo of globular clusters ( $\sim 2x$  the number of a spiral with similar luminosity)
- Colors of globular clusters show a bimodal distribution in ellipticals
- This is probably due to metallicity, so there is a population of metal poor and a population of metal rich GCs

E2



S0's

E3

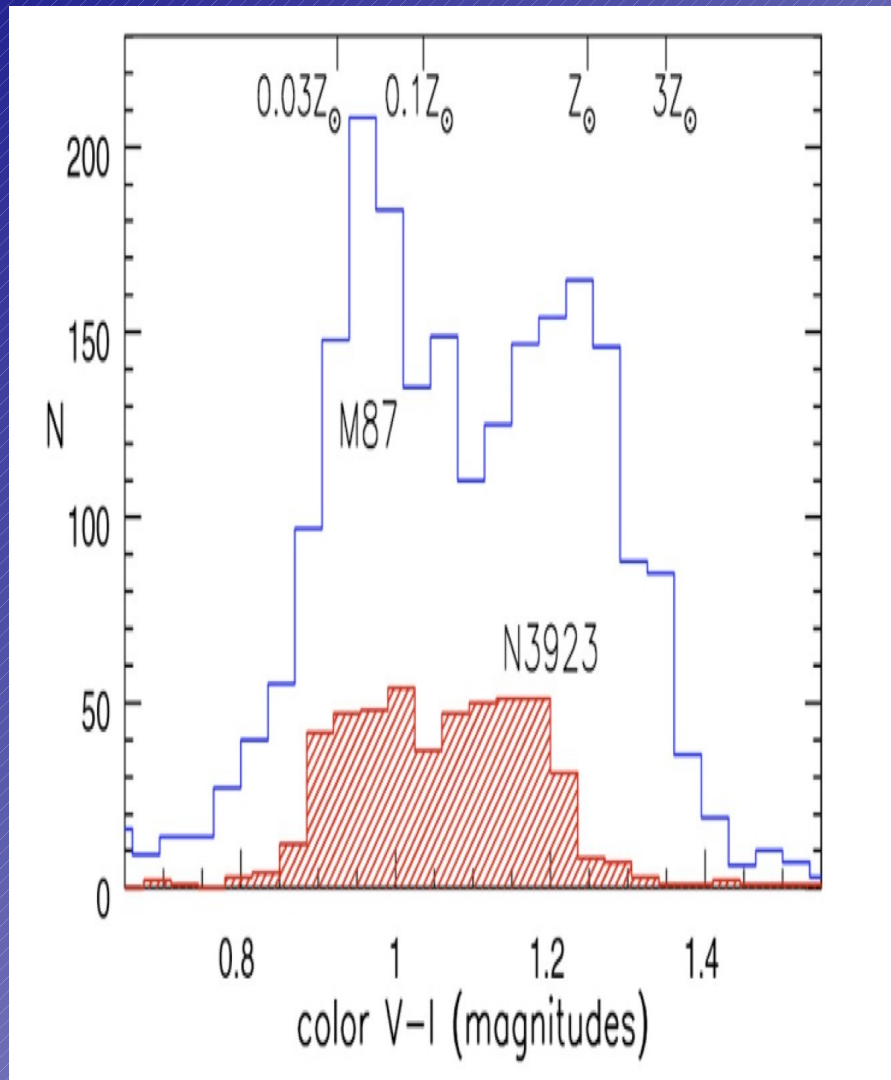


E5

Fig. 9.—  $B - R$  distributions for the early-type galaxy sample, including NGC 4472 from Paper I. For NGC 3379, the 36-object sample used to estimate the blue/red GC proportions is shown as a shaded histogram and the 50-object sample used as input to KMM is plotted with a solid line.

Rhode & Zeph (2004)  
What does this mean?

# Ellipticals & Globular clusters



- Generally ellipticals have 2x the globular clusters as spirals
- M87 has about 4x more globulars than N3923

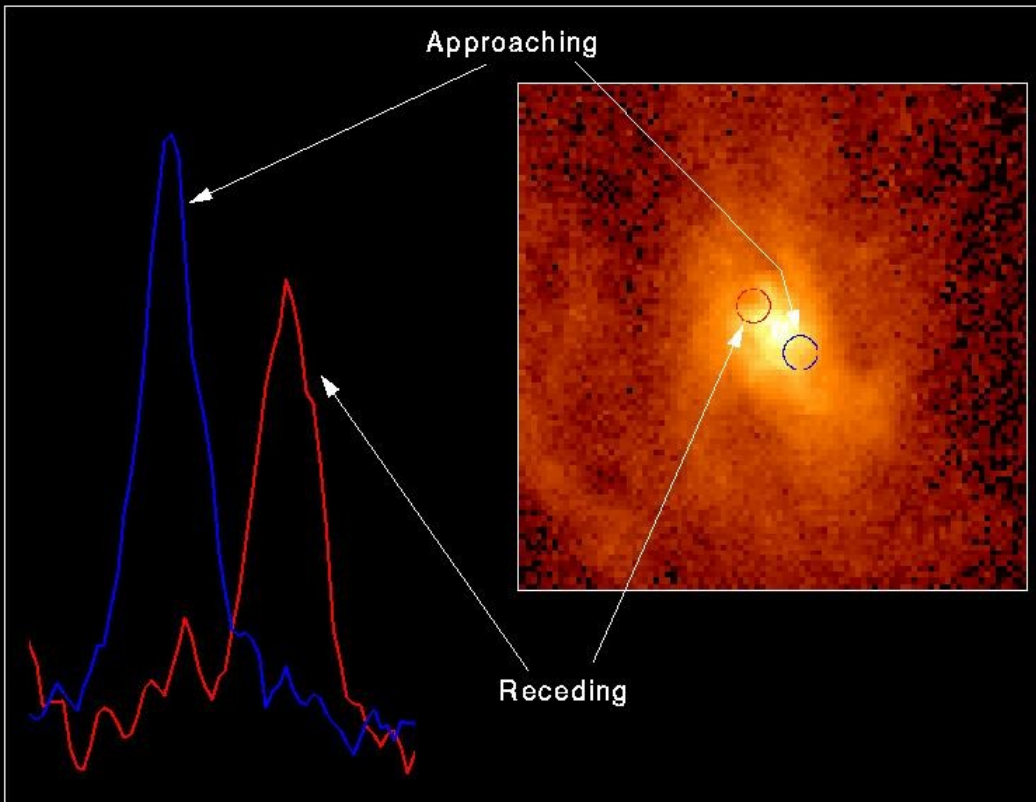


# Globular Clusters in Ellipticals cont.

- This could be caused by the
  - Merger of two galaxies - metal poor clusters are old, metal rich clusters formed during merger process
  - Hierarchical formation - Metal poor GC's are form at an early time and the metal rich population builds up during accretion of gas rich spirals

# Black Holes in Ellipticals

Spectrum of Gas Disk in Active Galaxy M87

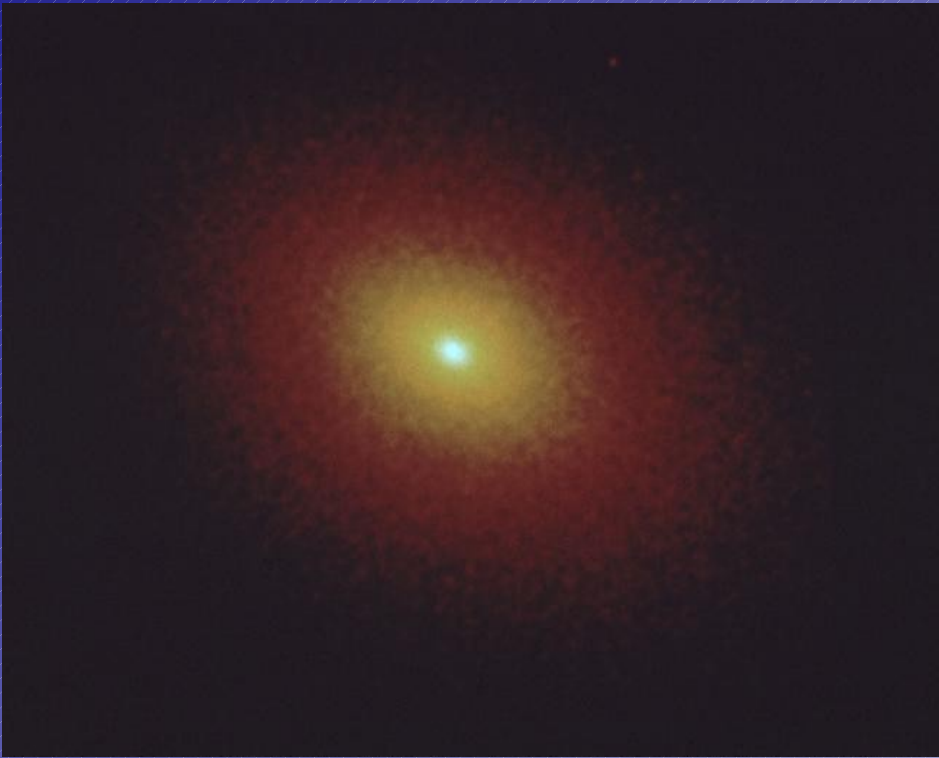


Hubble Space Telescope • Faint Object Spectrograph

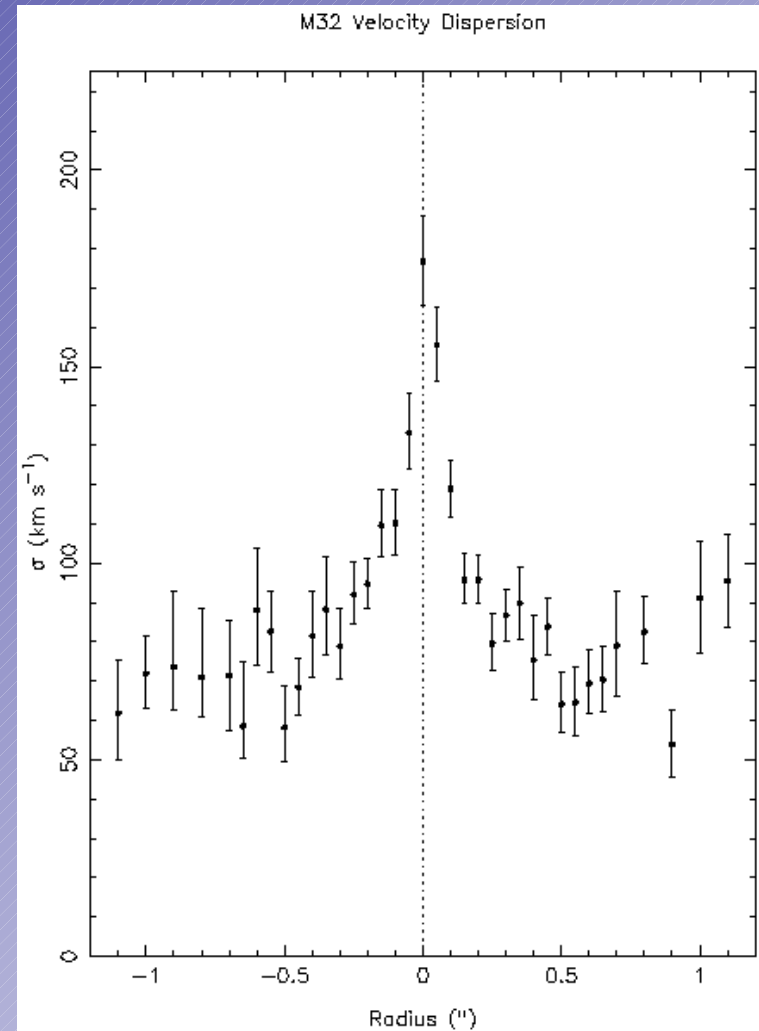


The first direct detection of gas being drawn into a BH. (Ford et al. 1994)

# Black Holes in Ellipticals cont.

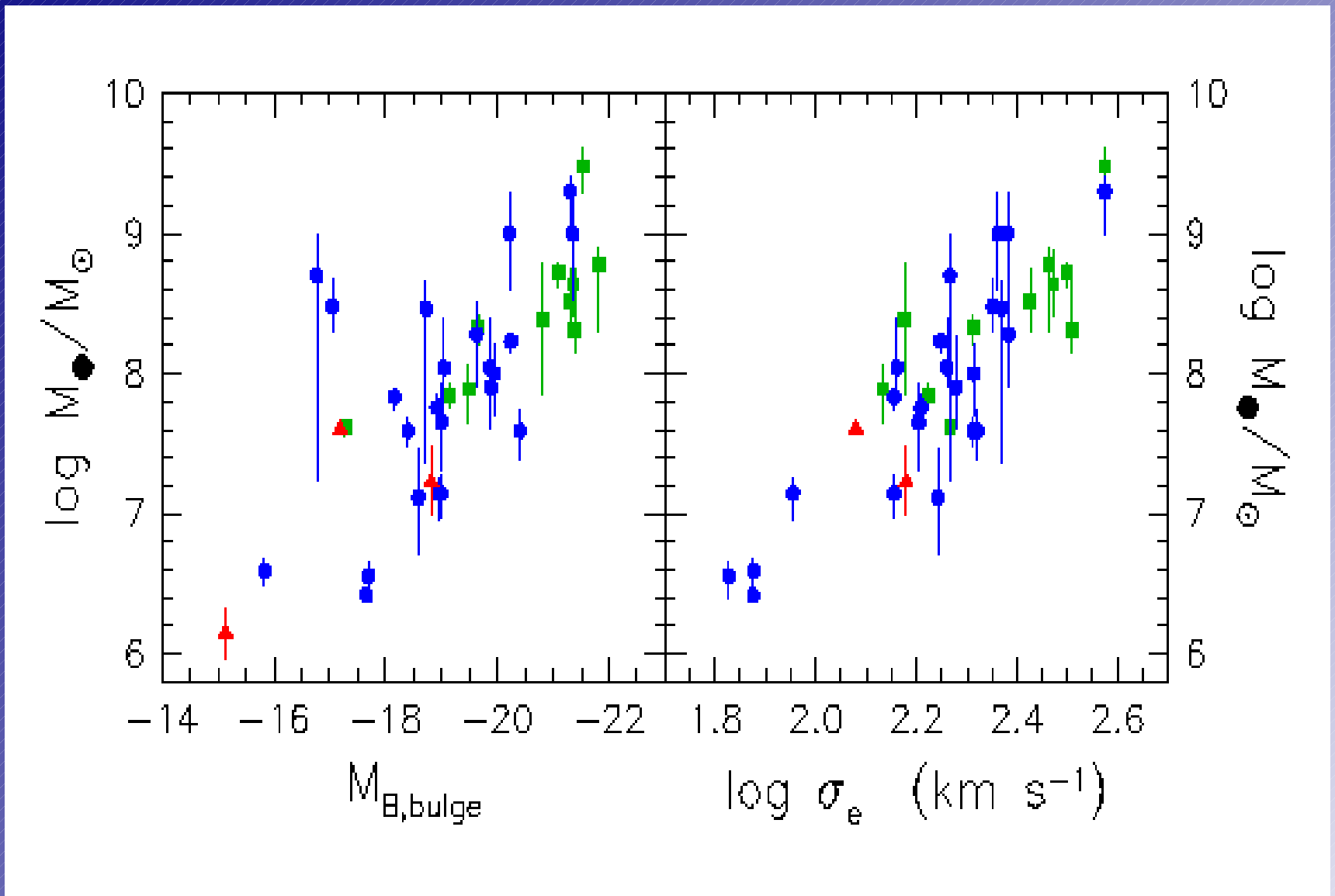


We can also infer the presence of a BH by looking at the stellar velocity dispersion in the nuclear region (M32).



# Black Holes in Ellipticals cont.

- Currently there are at least 40 BH candidates in nearby ellipticals and in the bulges of spirals
- There is a strong correlation between black hole mass and galaxy luminosity and velocity dispersion



Black Hole mass vs bulge mass and  $\sigma$  (Kormendy 2003)

# Why is this correlation so good?

- Observations imply BH mass 'knows' about the formation of bulges and ellipticals
  - All proto-galaxy clumps harbored a BH with the BH mass proportional to the bulge mass and BHs merged as the galaxy formed
  - BH started out small and grew as galaxy formed – e.g., central BH is fed during process of formation
    - Maybe act as the seed for the formation process (implies  $\rightarrow$  all galaxies have BHs)

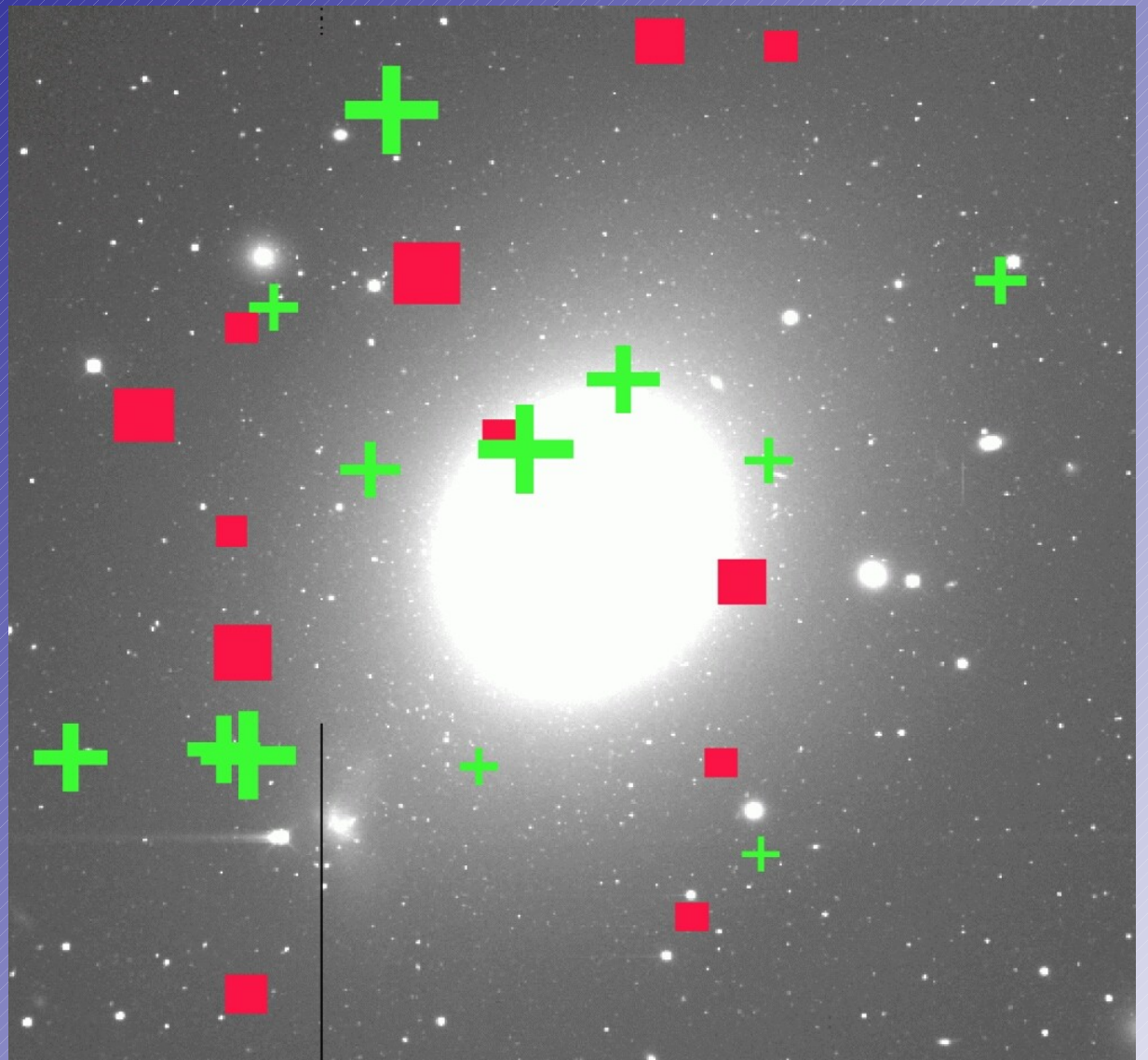
# Dark Matter in Elliptical Galaxies

- Looking at just the stars we expect the mass to light ratio of the stellar population to be  $M/L_V \sim 3-5$
- Orbital motions of the stars in the centers of ellipticals imply they are not dark matter dominated
- In the few ellipticals containing cold gas, we can measure the orbit of the gas we find  $M/L \sim 10 - 20$ 
  - But are these galaxies typical of all E's
- Also can use the amount of mass required to retain the hot x-ray gas, find  $M/L \sim 100$  for galaxies with large x-ray halos
  - Mostly Luminous and midsized ellipticals

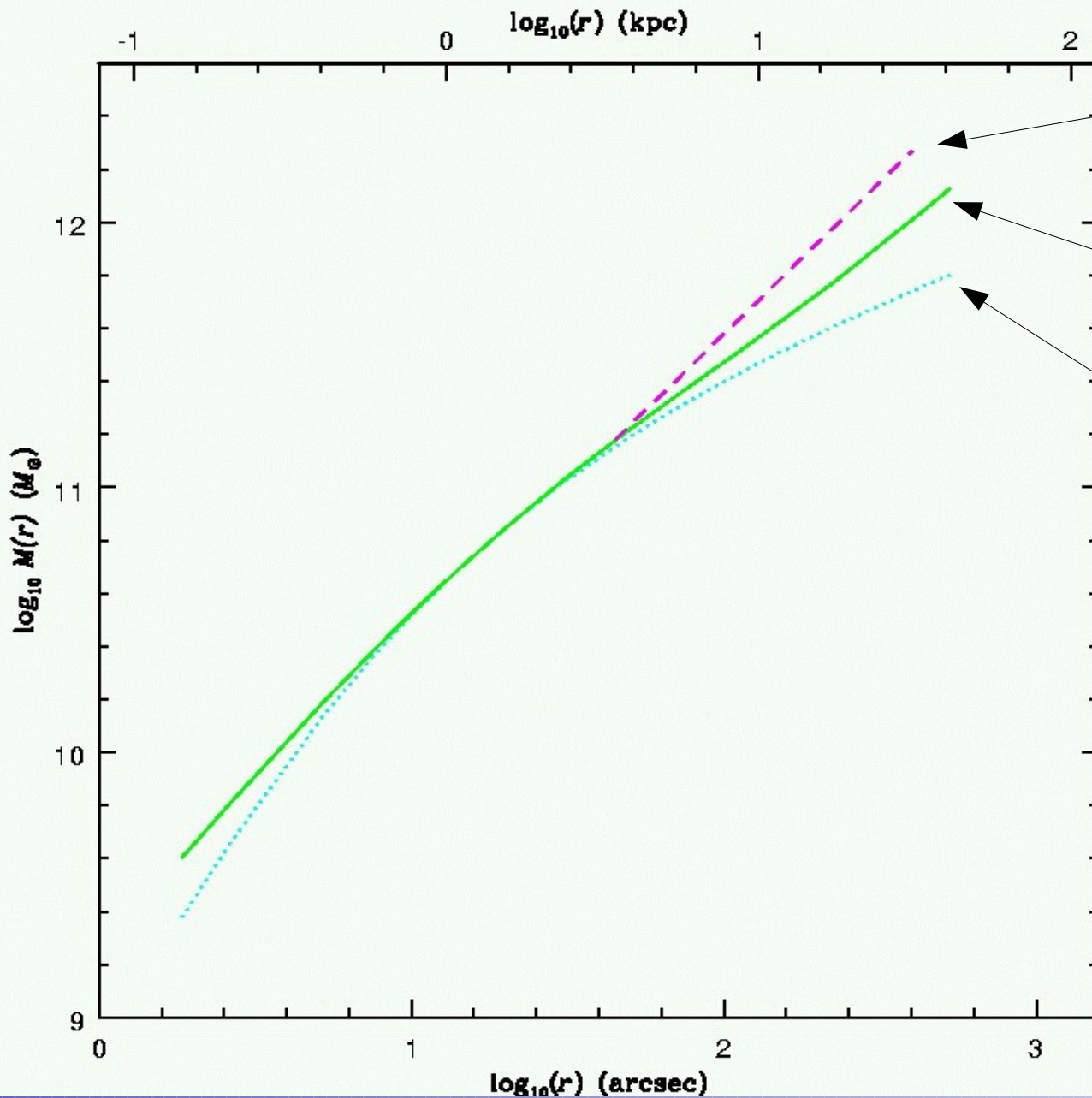
# Dark Matter in Elliptical Galaxies cont.

- Are there any other ways to look at velocities?
  - globular clusters and planetary nebulae
  - Recent results of PN dynamics around (a few) elliptical galaxies show NO dark matter, the galaxies are “naked”
  - Recent results of GC dynamics around (a few) elliptical galaxies show large dark halo.





PN velocities in NGC 4472, + is blueshifted, - is redshifted. (Romanowsky 2001)

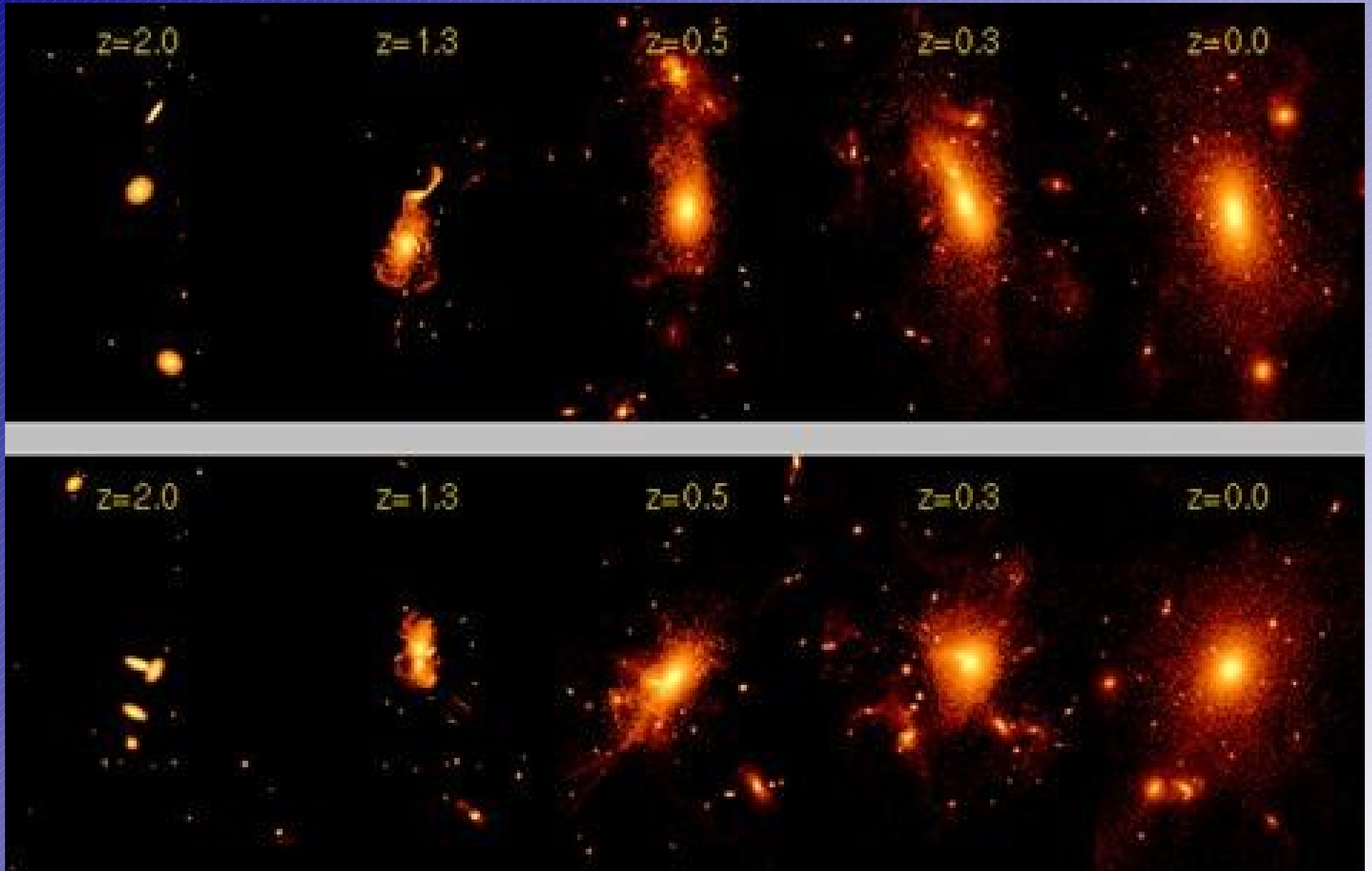


Mass from  
Stars & M/L

Mass from  
PN & Stars

Mass from  
GC velocities

# Formation of Ellipticals



# Formation of Ellipticals cont.

- Equal mass mergers can account for the massive ellipticals with boxy isophotes and little rotation
- Unequal mass mergers can explain less massive ellipticals with disky isophotes and higher rotation